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# Recent Results in Resilient CPS Design using Passivity and Dissipativity

Current Research by Panos Antsaklis' Group at Notre Dame:

Hasan Zakeri

Yang Yan

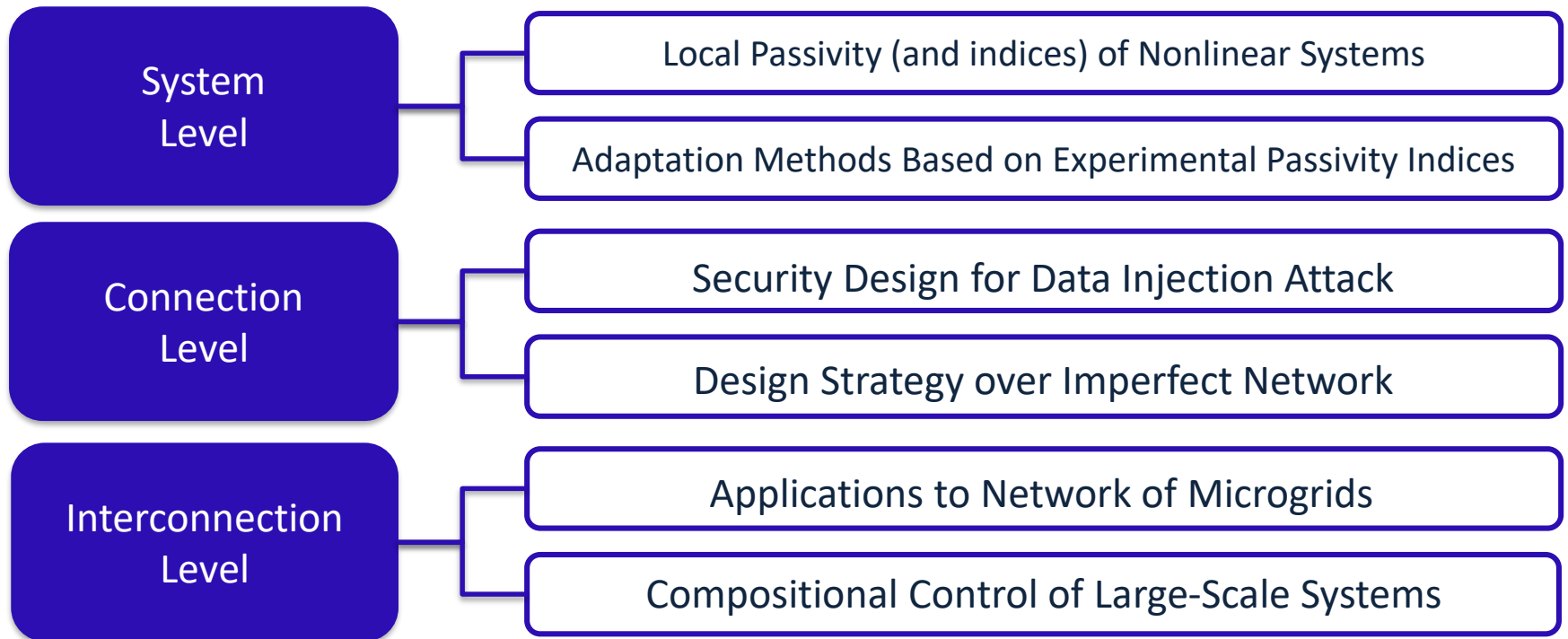
Etika Agarwal

Control Systems and the Quest for Autonomy

28<sup>th</sup> October, 2018

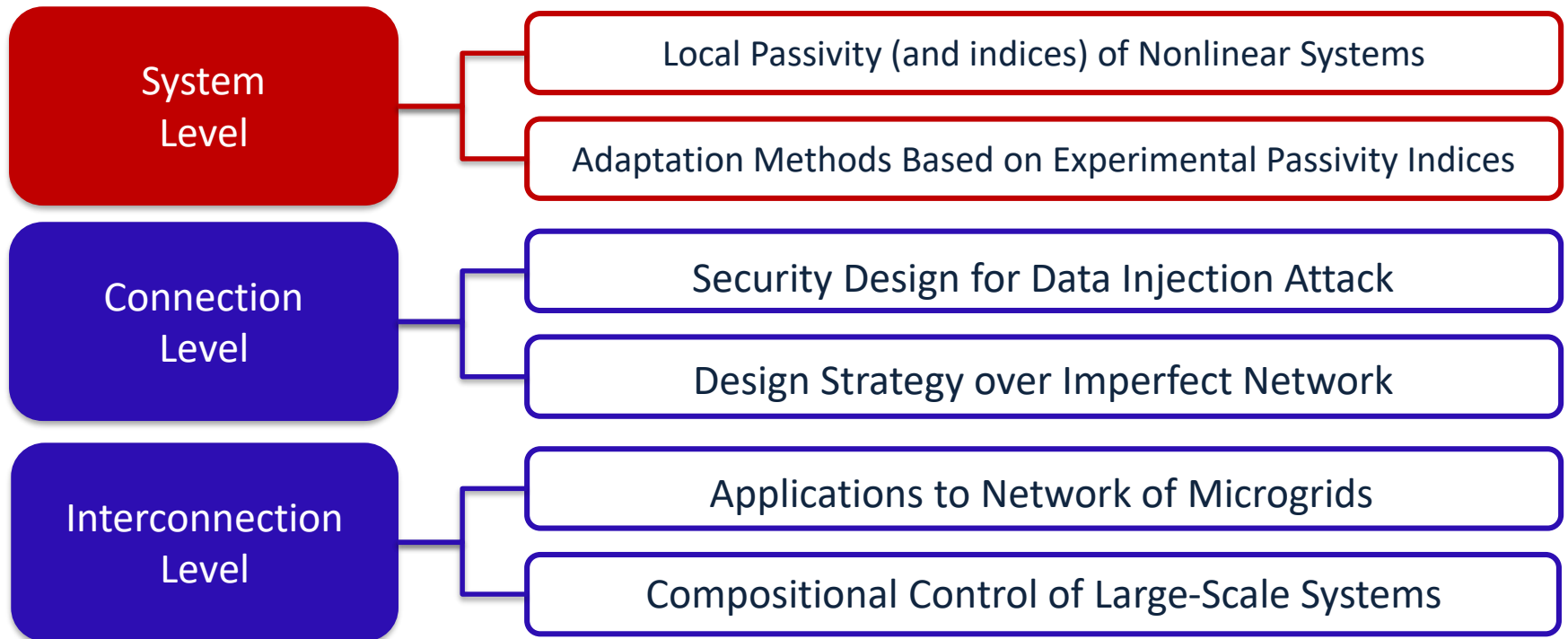
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# Overview



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# Local Passivity Indices of Nonlinear Systems

- Behaviors of nonlinear systems change in different regions
- Examples: stability, controllability, and even uniqueness and existence
- Even systems that are passive around one equilibrium and non-passive around another
- Limited course of action in most physical systems bounded control input
- Controllers and feedback loops “tame” the system to operate around an equilibrium
- Solution: studying IO properties (particularly passivity indices) with respect to regions of state space and known bounds on input signal
- New definitions for passivity indices with respect to restrictions on the state and input spaces

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# Example

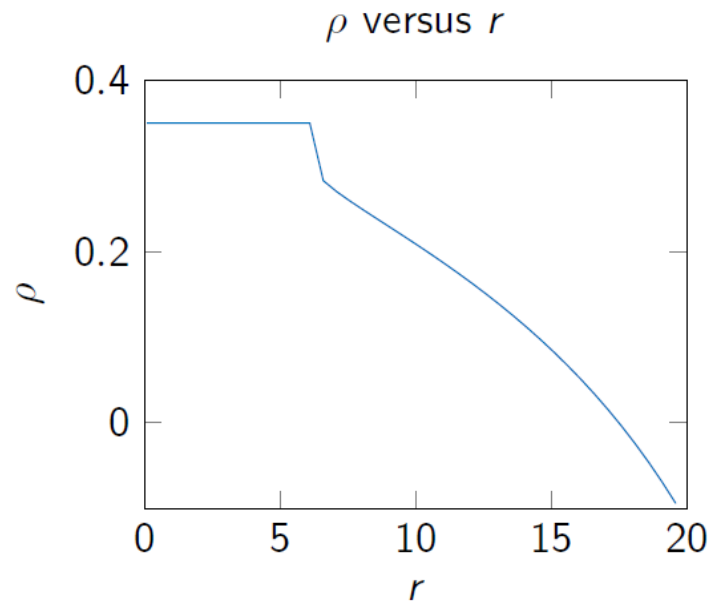
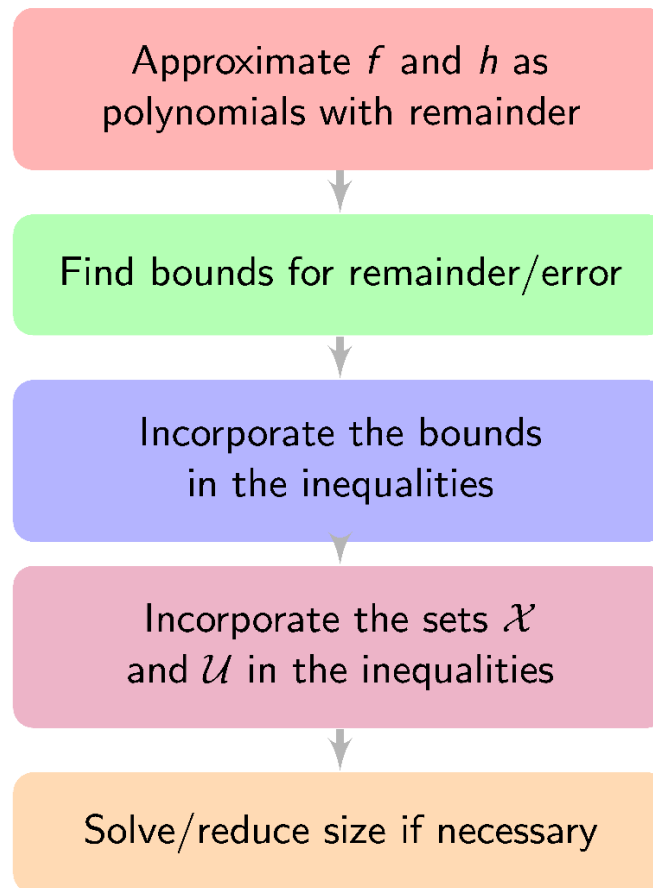


Figure: OFP index  $\rho$ , for  $X = \{x \mid \|x\|_2^2 \leq r\}$

For an example nonlinear system

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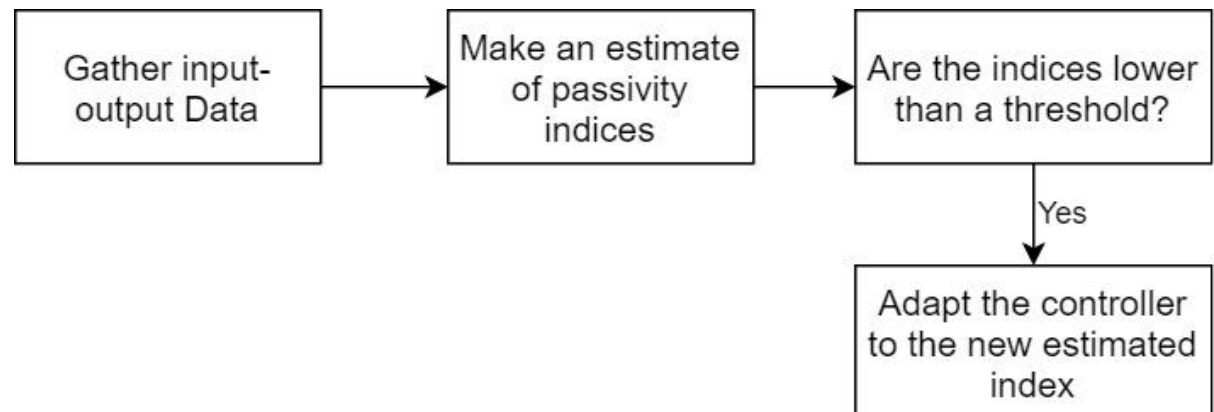
# Approximate Methods For Passivity Indices



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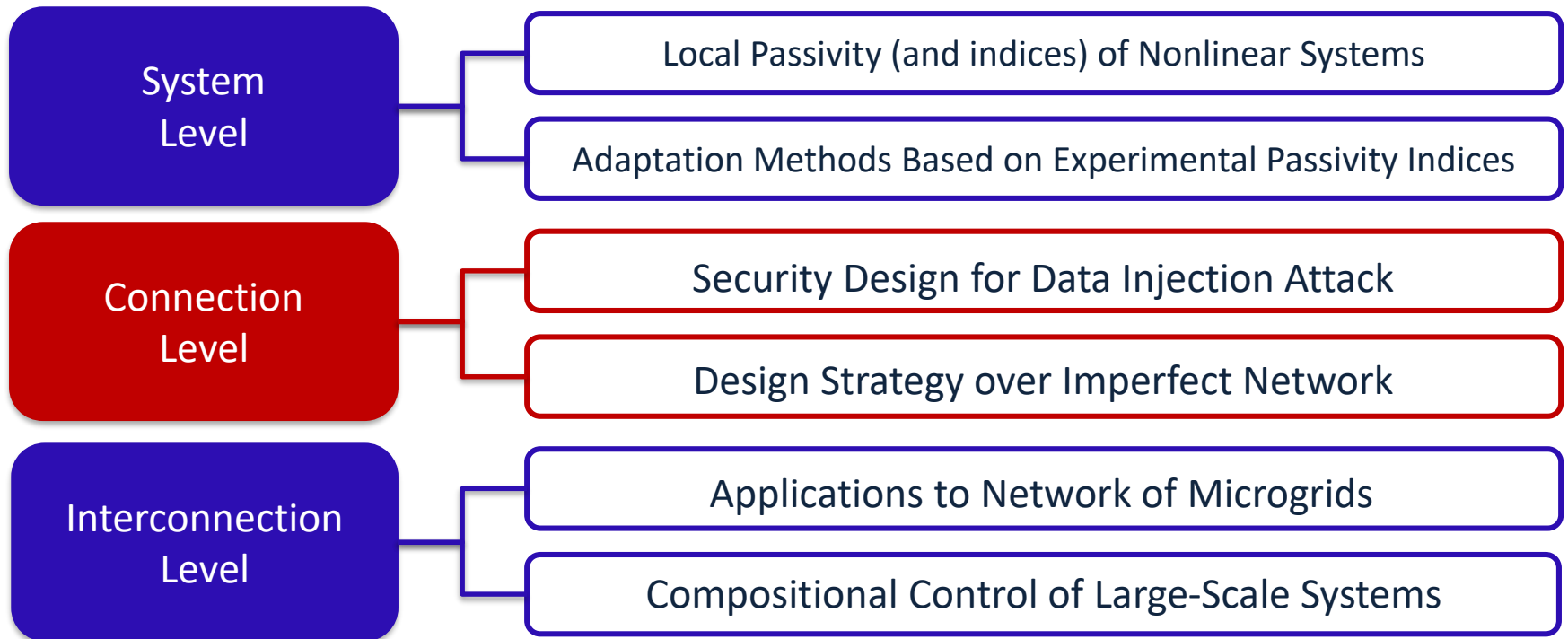
# Adaptation Method Based on Experimental Passivity Indices

- Experimental passivity indices of the system (with respect to current input)
- A measure of failure in the system (data-driven, no model)
- Adaptive method to mitigate any shortage with changing the controller



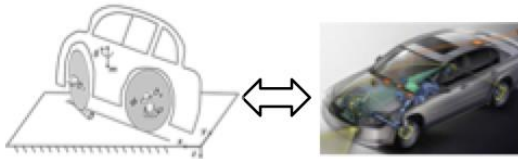
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# Overview

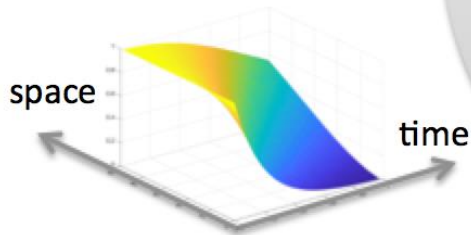




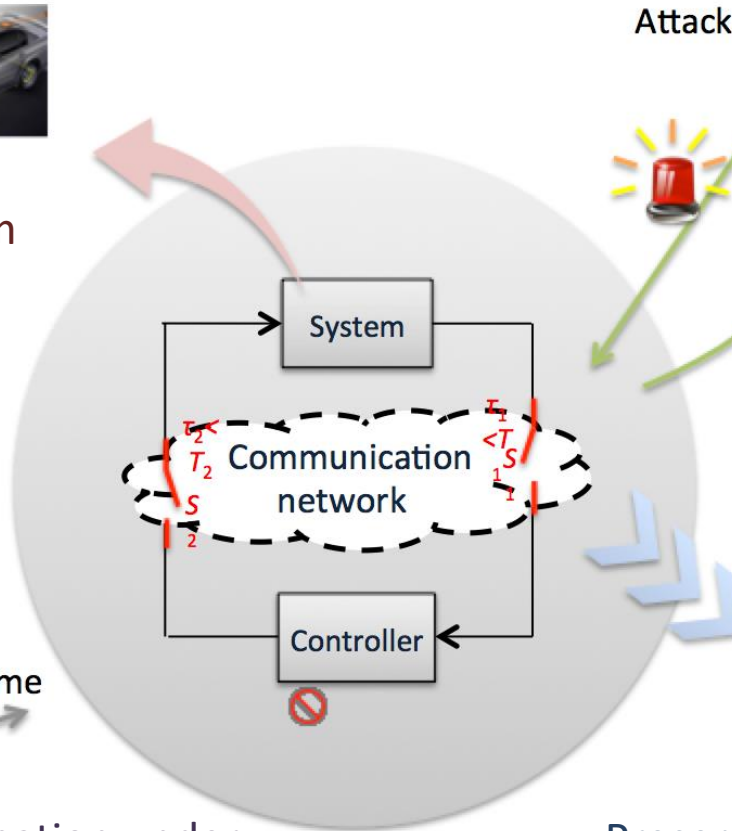
# Challenge in Connection Level



Analyze behavior from its approximation considering model discrepancies



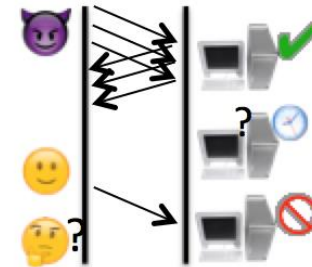
Analyze energy dissipation under a digital control framework for high-dimensional systems



Attack / Disturbance

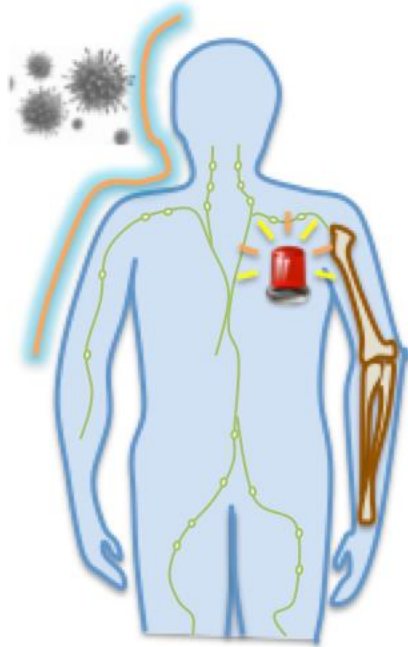


Design a joint disturbance monitor and robust controller framework facing uncertainties and adversarial attacks



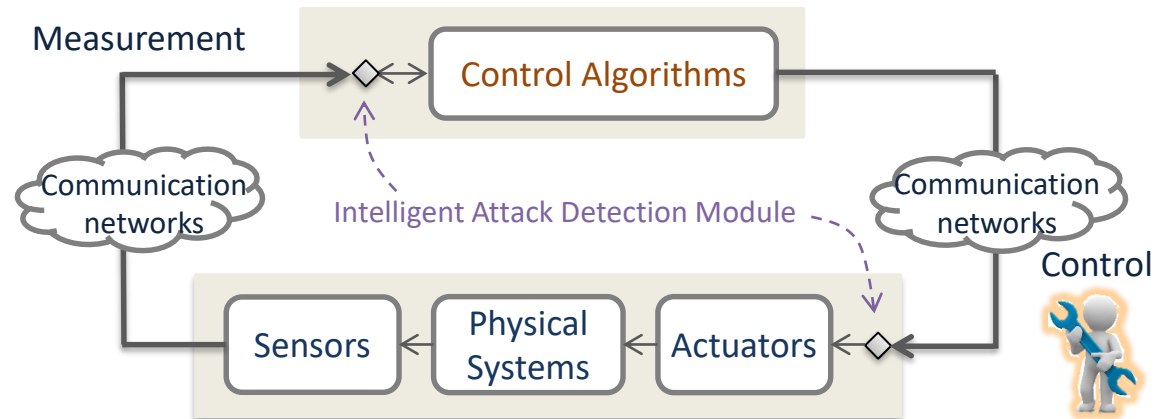
Preserve passivity and stability properties over imperfect communication networks

# Joint Disturbance Observer and Controller Design



The **immune system** (from the Latin work *immunis*, meaning: “untouched”) protects the body like a guardian from harmful influences from the environment and is essential for survival\*.

\* U.S. National Library of Medicine, “Immune System”. <https://www.ncbi.nlm.nih.gov/pubmedhealth/>.



Y. Yan, P. Antsaklis and V. Gupta, “A resilient design for cyber physical systems under attack,” *2017 American Control Conference (ACC)*, Seattle, WA, 2017, pp.4418-4423.

# Joint Disturbance Observer and Controller Design

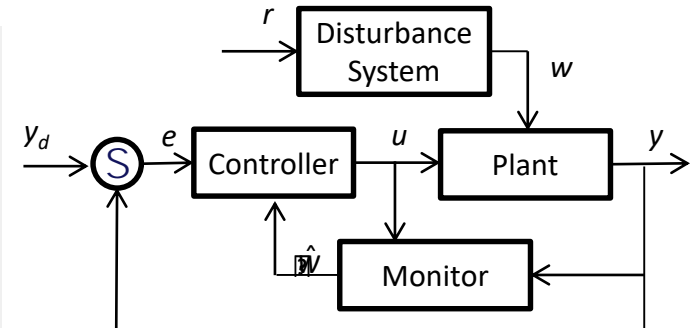
## Attack Monitor:

Internal state variable  $\rightarrow \dot{\varepsilon} = -l(x)\varepsilon + l(x)(-Ax - Bu - \rho(x))$

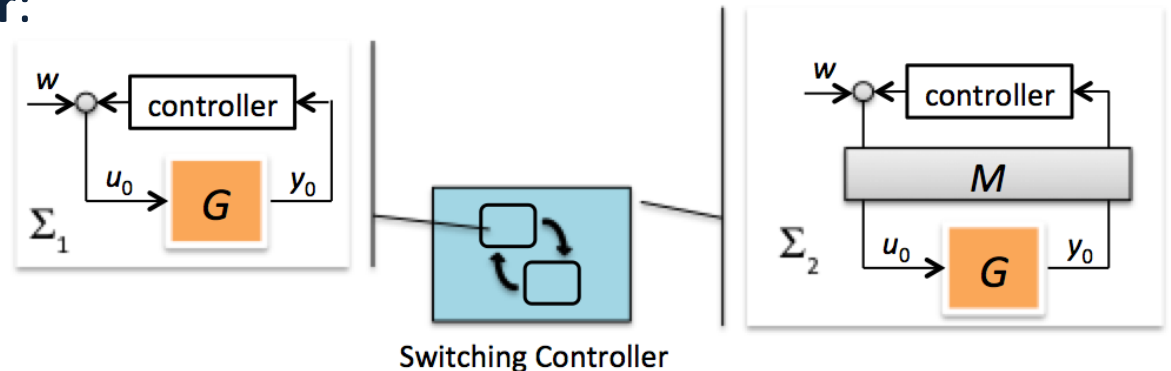
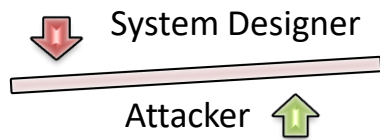
Output of the detection filter  $\rightarrow \hat{w} = \varepsilon + \rho(x)$

Detection filter gain  $\rightarrow \frac{d}{dt}\rho(x) = l(x)\dot{x}$

Nonlinear function to be designed



## Switching the controller:



LMI of stable performance under attack

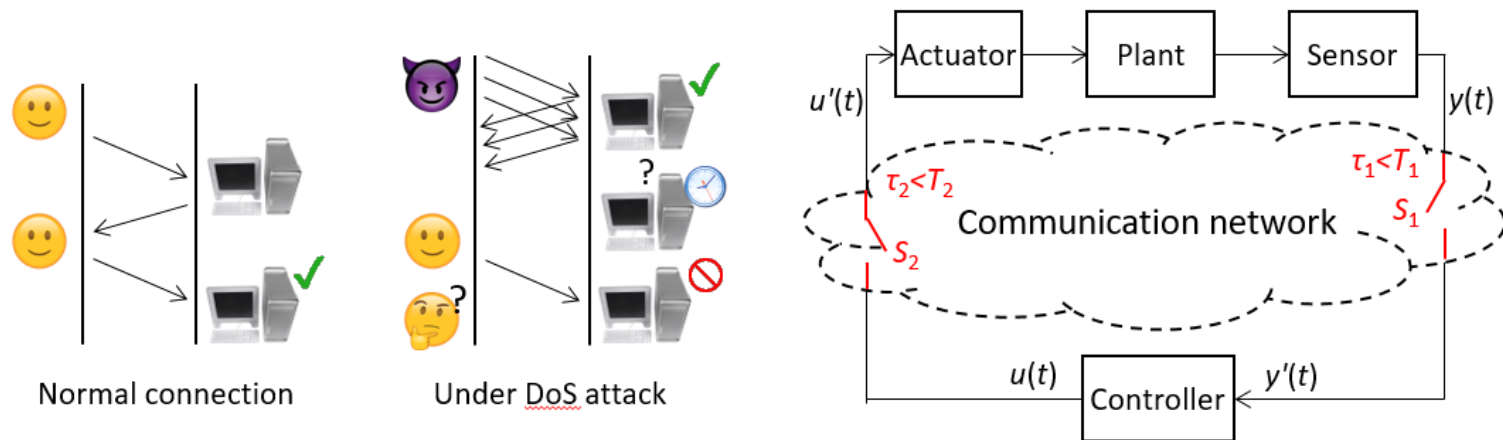


Design passivation linear transformation  $M$

# Self-Triggered Strategy under DoS Attack

A **denial-of-service (DoS attack)** is a cyber-attack where the perpetrator seeks to make a machine or network resource unavailable to its intended users by temporarily or indefinitely disrupting services of a host connected to the Internet\*.

\* “Understanding Denial-of-Service Attacks”. *US-CERT*. <https://www.us-cert.gov/ncas/tips/ST04-015> Retrieved Dec 8<sup>th</sup> 2017.



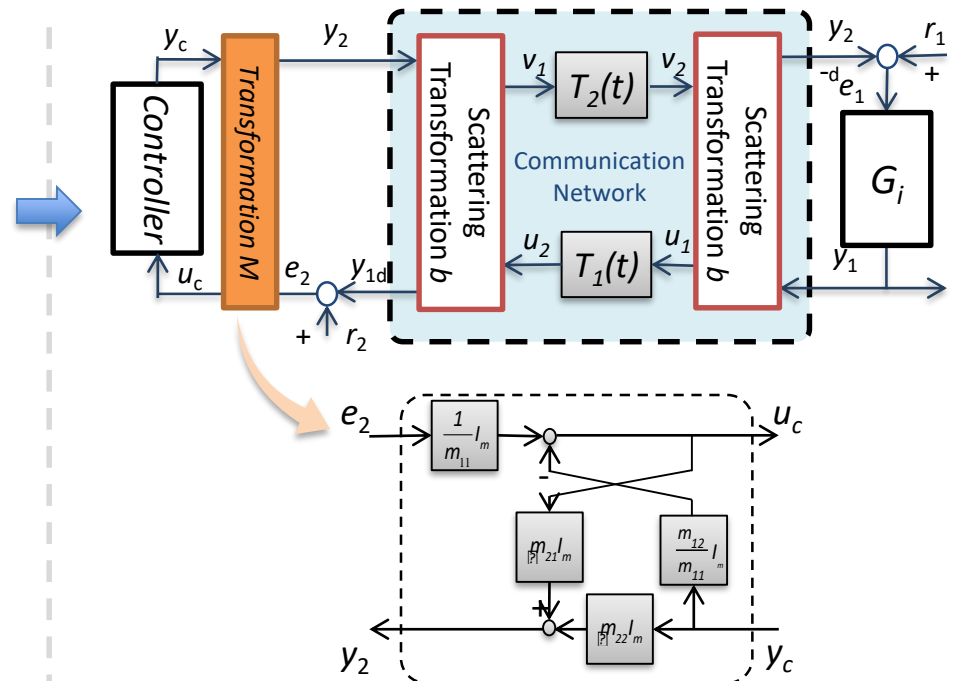
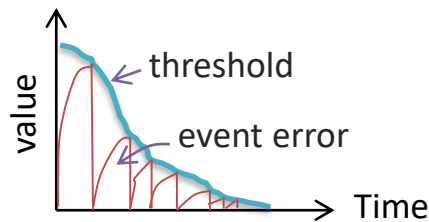
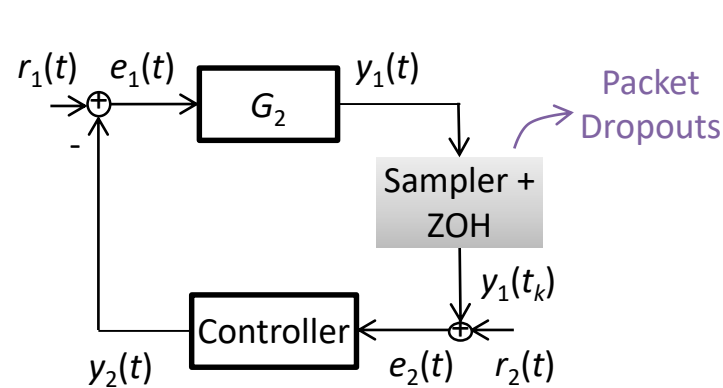
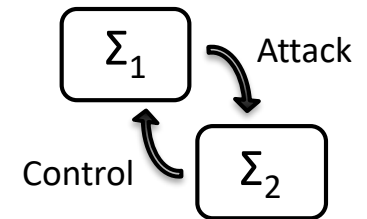
Y. Yan, M. Xia, A. Rahnama and P. Antsaklis, “A passivity-based self-triggered strategy for cyber physical systems under denial-of-service attack,” *2017 IEEE 56<sup>th</sup> Annual Conference on Decision and Control (CDC)*, Melbourne, VIC, 2017, pp. 6072-6088.

# Self-Triggered Strategy under DoS Attack

**Attack** : communication through the network is not ideal

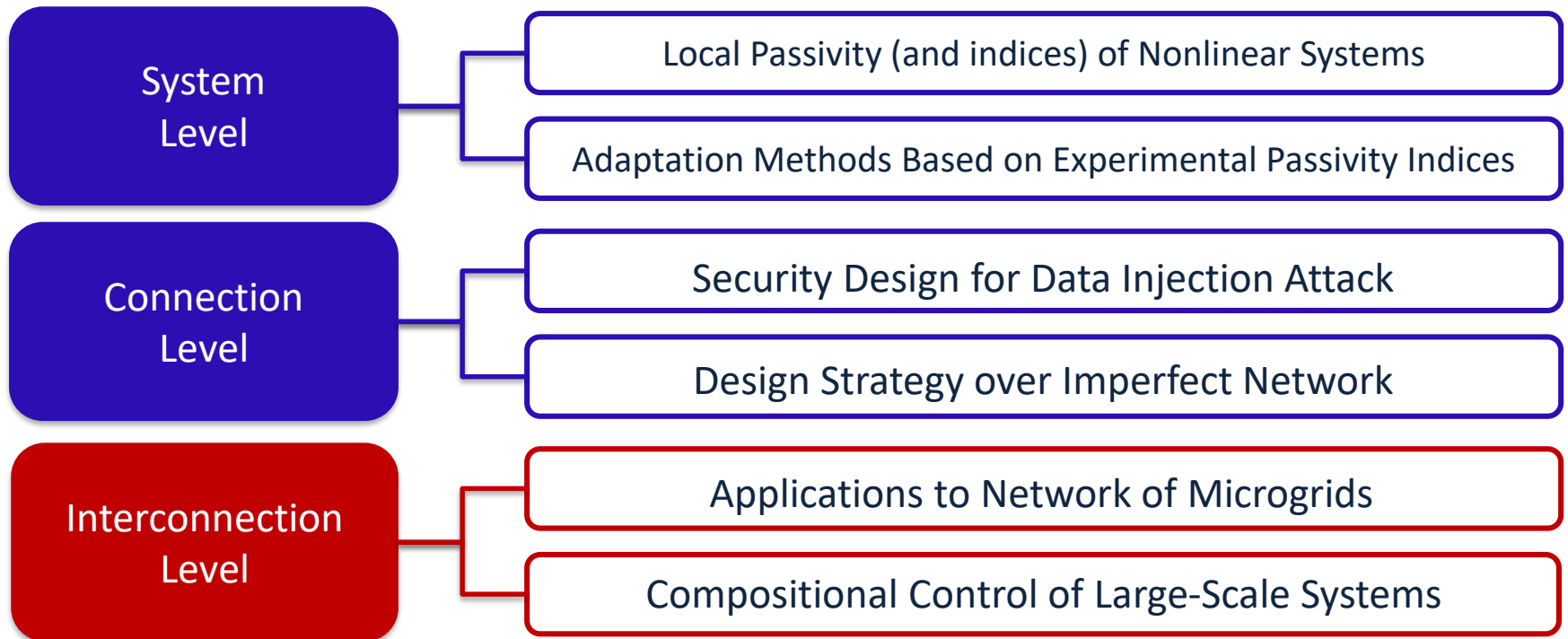
**Objective** :

- Maximum tolerable length of attack
- Switching strategy

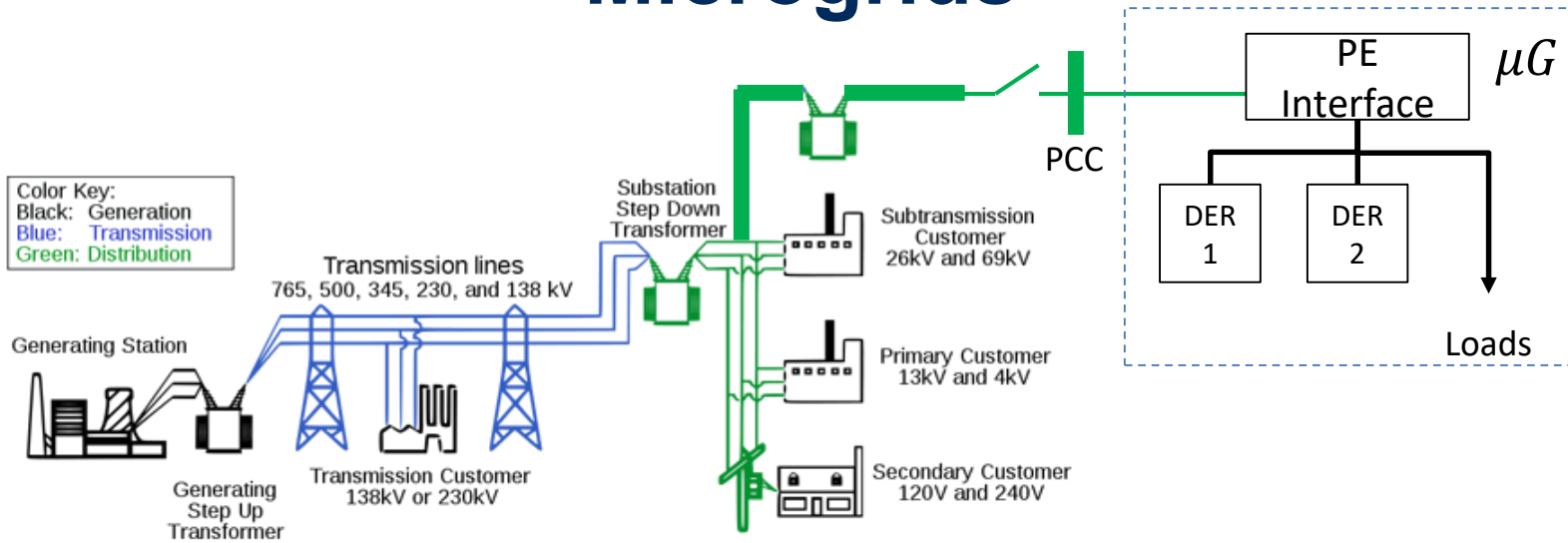


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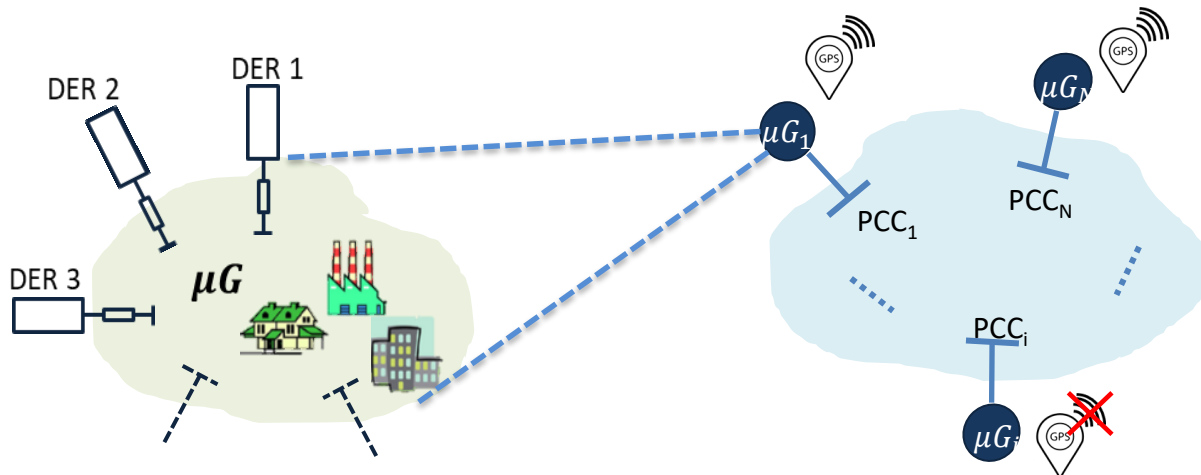
# Overview



# Microgrids

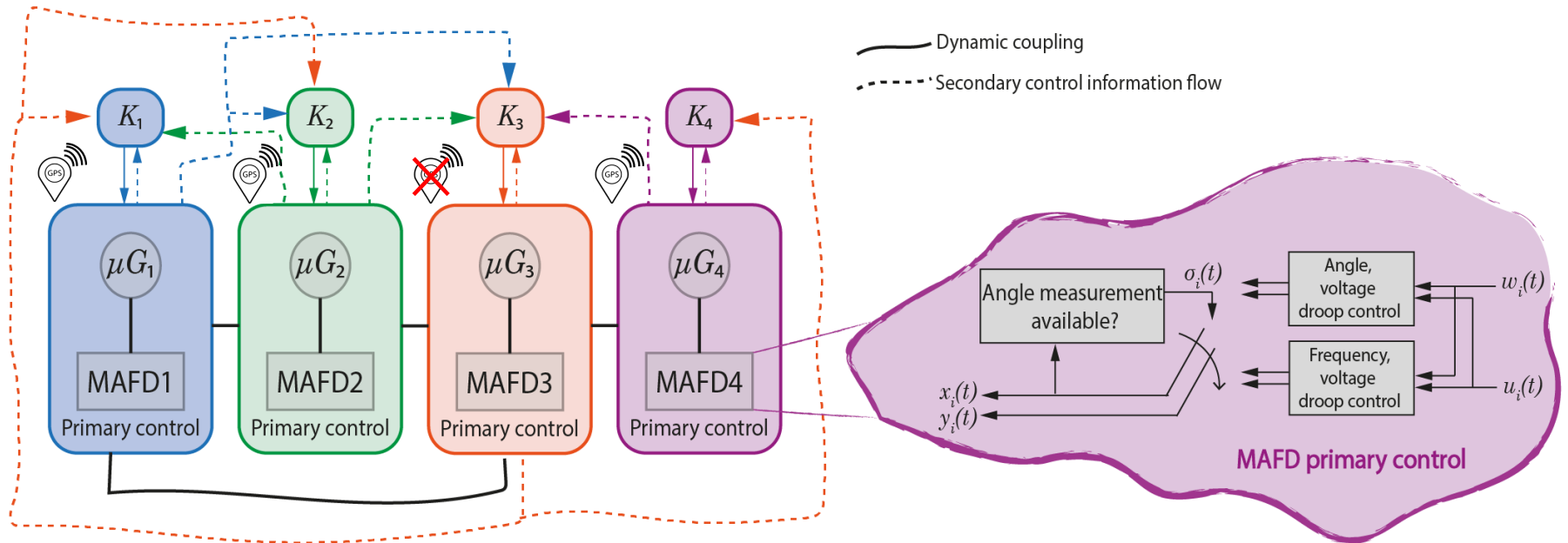


**Inter-grid**



**Intra-grid**

# Distributed Mixed Voltage Angle and Frequency Droop Control of Microgrid Interconnections with Loss of Distribution-PMU Measurements



## D-MAFD

- Passivity under loss of PMU-measurement
- Robustness to topology changes

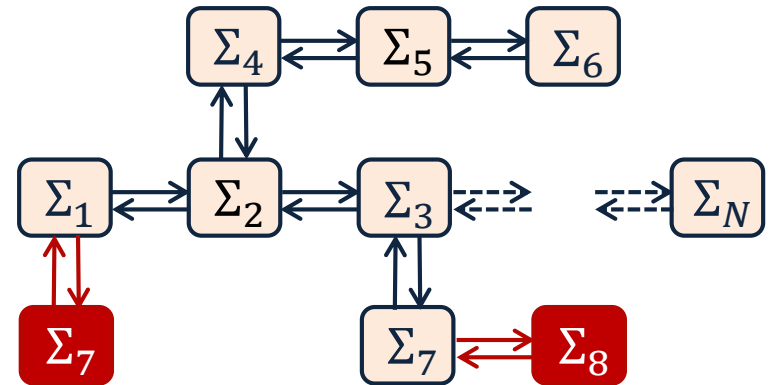
**Next question – How do we facilitate ad-hoc connections of microgrids?**

S. Sivarajani\*, E. Agarwal\*, L. Xie, V. Gupta, and P. J. Antsaklis, "Distributed mixed voltage angle and frequency droop control of microgrid interconnections with loss of distribution-PMU measurements," submitted to IEEE Transactions on Smart Grid, arXiv:1810.09132, Oct 2018.



# Compositional Control of Large-Scale Systems

*“We refer to a system as large-scale if it is more appropriate to consider the system as an interconnection of small sub-systems than dealing with it as a whole”*

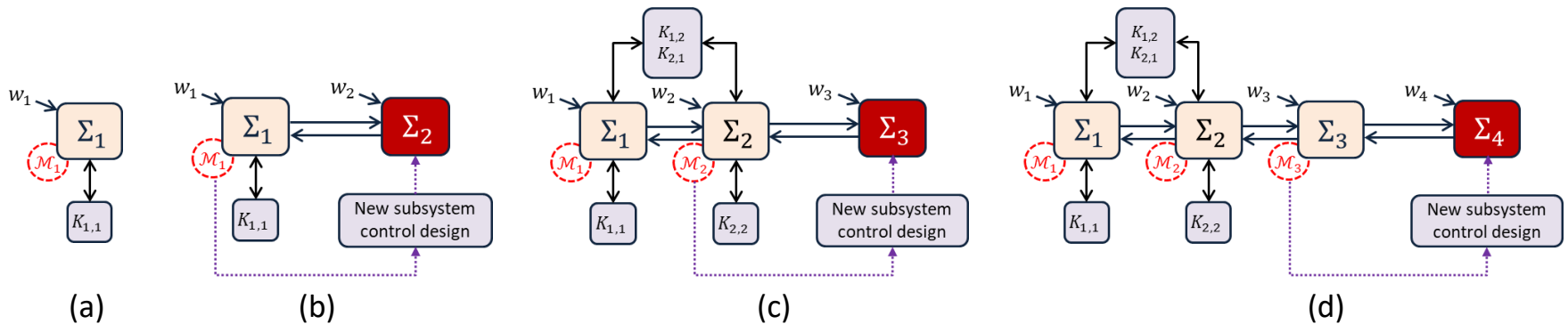
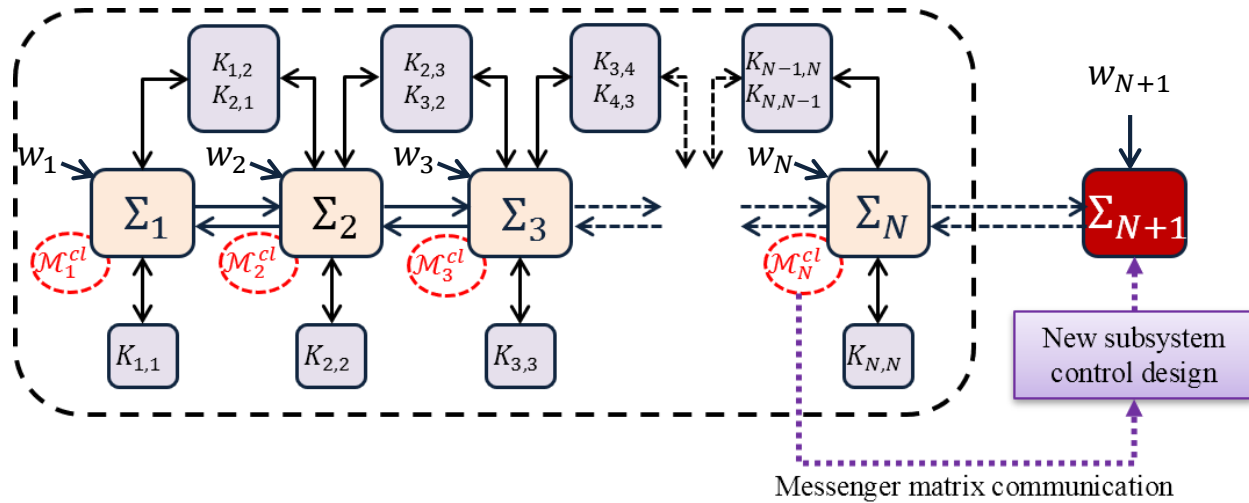


## **Objective:**

Develop an algorithm to guarantee passivity of a dynamically growing interconnection, such that the addition of new subsystems does not require redesigning the pre-existing local controllers in the network.

- Distributed verification of passivity using equivalent analysis on passivity of individual subsystems and coupling at individual interconnections.
- Local synthesis of individual sub-system level controllers, with no direct knowledge of the dynamics of other subsystems, for passivity guarantees on large-scale system.

# Sequential Synthesis of Distributed Controllers for Cascade Interconnected Systems

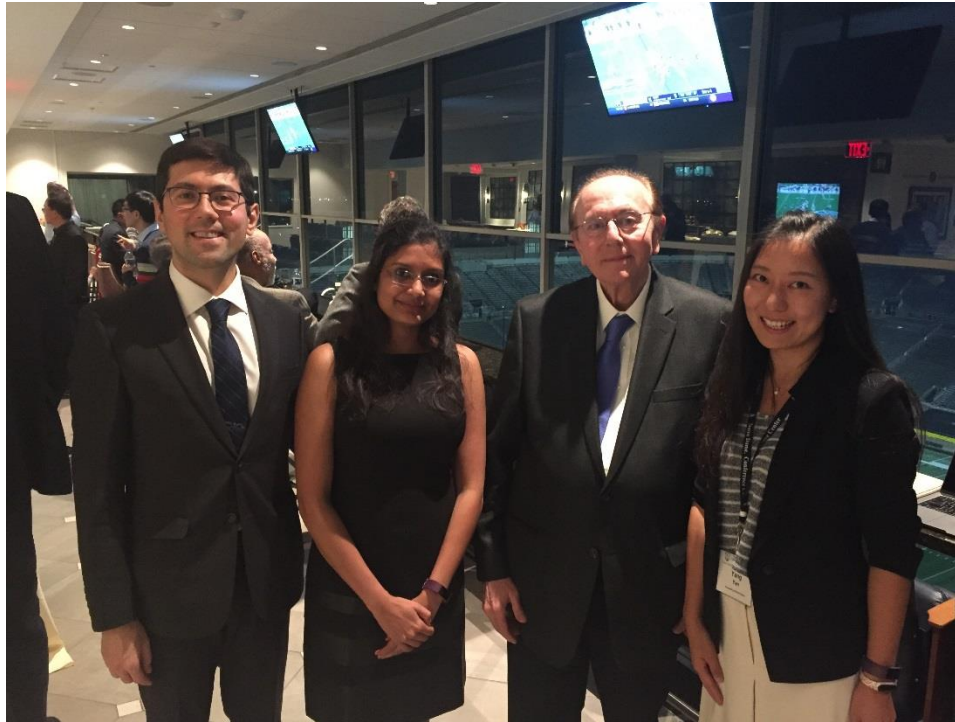


E. Agarwal\*, S. Sivaranjani\*, V. Gupta, P. J. Antsaklis, "Sequential synthesis of distributed controllers for cascade interconnected systems," submitted to American Control Conference, 2019, pre-print: [goo.gl/JTCV6z](http://goo.gl/JTCV6z).

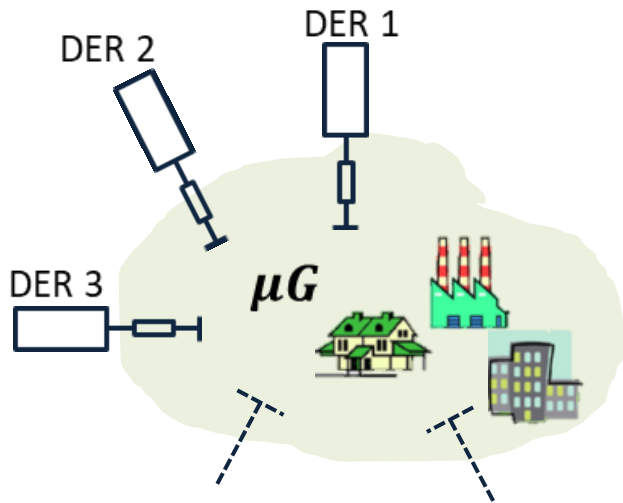
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# Thank You

## For always being there for us, and for all your mentorship

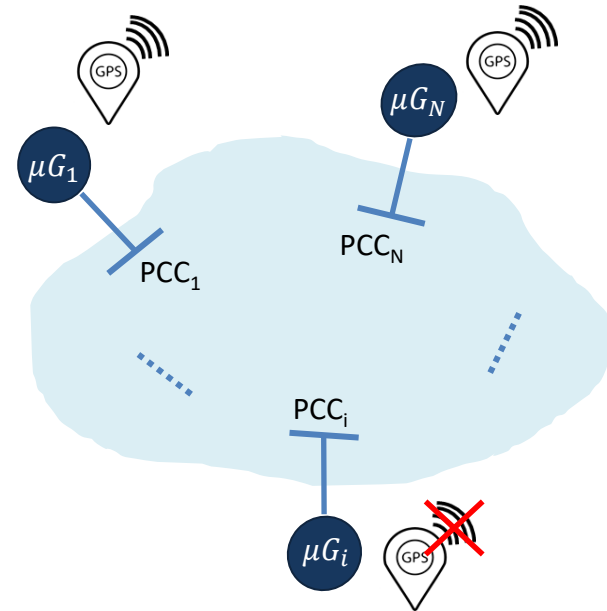


# Microgrids



## Intra -grid

- Stability with respect to small disturbances
- Robustness to generation-load mismatch
- Information and network limitations



## Inter -grid

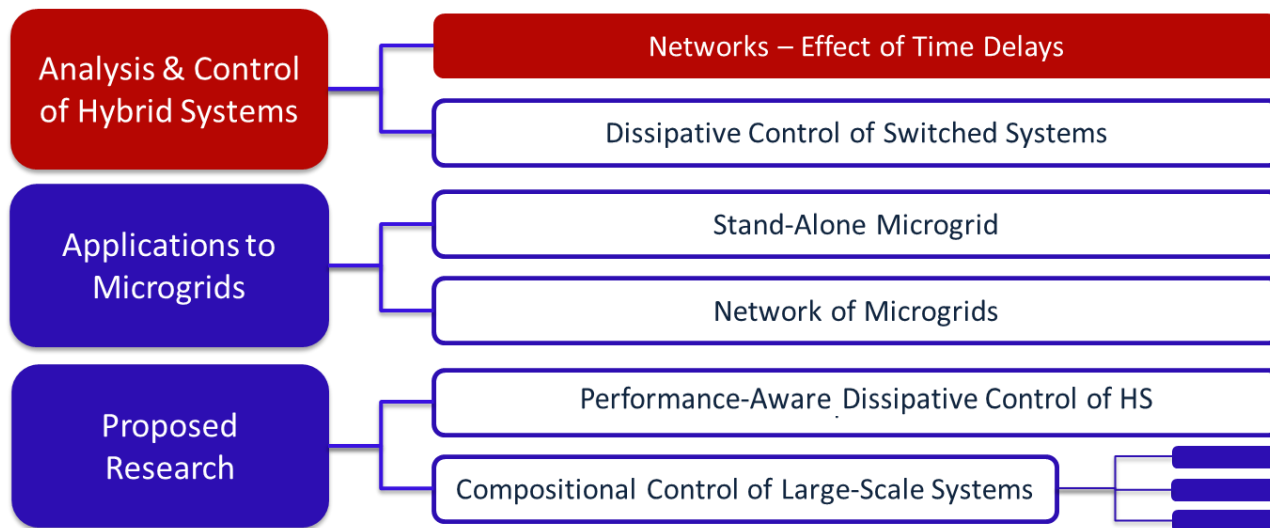
- PMU-measurement loss
- Robustness to topology changes
- Facilitate ad-hoc connections of microgrids

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# Dissipativity of Networks of Hybrid Systems

E. Agarwal, M. J. McCourt, and P. J. Antsaklis, "Dissipativity of hybrid systems: Feedback interconnections and networks," in American Control Conference (ACC), 2016. IEEE, 2016, pp. 6060-6065.

E. Agarwal, M. J. McCourt, and P. J. Antsaklis, "Dissipativity of finite and hybrid automata: An overview," in Control and Automation (MED), 2017 25<sup>th</sup> Mediterranean Conference on. IEEE, 2017, pp. 1176-1182.



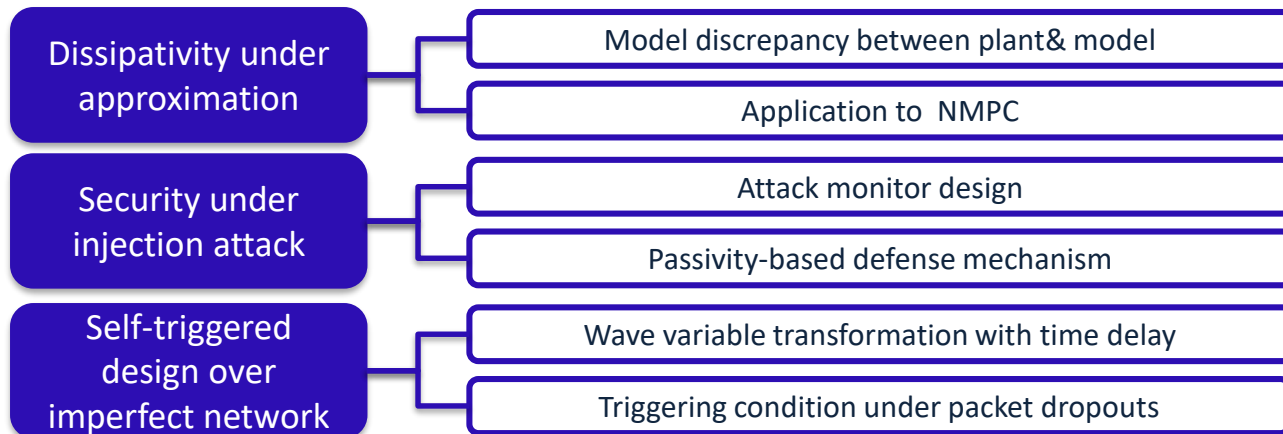
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# Resilient Design for Connection Level

**Yang Yan** and Panos Antsaklis, “Stabilizing Nonlinear Model Predictive Control Scheme Based on Passivity and Dissipativity,” *2016 American Control Conference (ACC)*, Boston, MA, 2016, pp.76-81.

**Y. Yan**, P. Antsaklis and V. Gupta, “A resilient design for cyber physical systems under attack,” *2017 American Control Conference (ACC)*, Seattle, WA, 2017, pp.4418-4423.

**Y. Yan**, M. Xia, A. Rahnema and P. Antsaklis, “A passivity-based self-triggered strategy for cyber physical systems under denial-of-service attack,” *2017 IEEE 56<sup>th</sup> Annual Conference on Decision and Control (CDC)*, Melbourne, VIC, 2017, pp. 6072-6088.



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# Dissipativity

The system (1) is said to be dissipative with respect to the supply rate  $\omega(w(t), y(t))$ , if there exists a positive definite function  $V(x): \mathbb{R}^n \rightarrow \mathbb{R}^+$  with  $V(0) = 0$ , called the storage function, such that

$$\int_{t_0}^{t_1} \omega(w(t), y(t)) dt \geq V(x(t_1)) - V(x(t_0))$$

holds, for all  $w \in \mathbb{R}^m$ , and all  $t_1 \geq t_0 \geq 0$ , where  $x(t_1)$  is the state at time  $t_1$  resulting from the initial condition  $x(t_0)$  and input  $w(\cdot)$ .

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# Dissipativity

Supply rate	Dissipativity
	– Dissipativity
	Passivity
	State Strict Passivity;
	Input Feed-Forward Passivity (IFP); ISP if
	Output Feedback Passivity (OFP); OSP if
	Finite Gain stability,

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Passivity, ISP, OSP

State Strict Passivity

– Dissipativity,

OSP

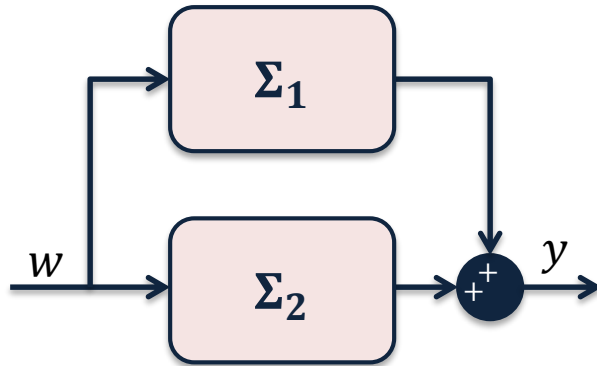
Lyapunov Stability

Asymptotic stability

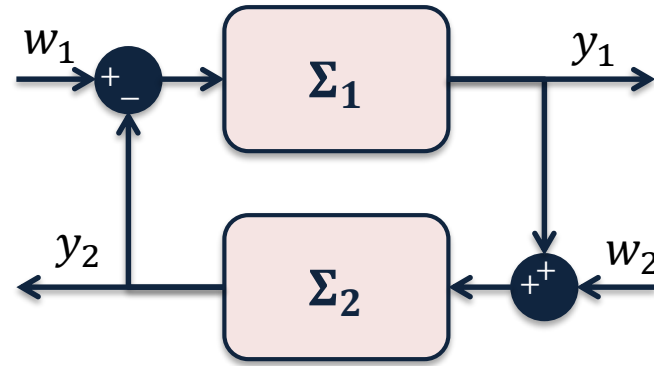
Finite Gain Stability

Finite Gain Stability

# Dissipativity



$\Sigma_1$  - Passive/ISP  
 $\Sigma_2$  - Passive/ISP



$\Sigma_1$  - *QSR* dissipative  
 $\Sigma_2$  - *QSR* dissipative

Passivity, ISP, OSP

State Strict Passivity

– Dissipativity,

OSP

Lyapunov Stability

Asymptotic stability

Finite Gain Stability

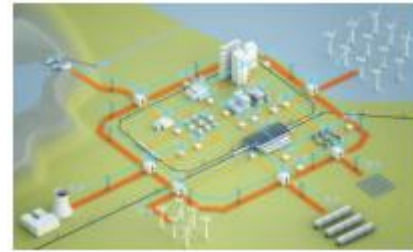
Finite Gain Stability

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# Cyber-Physical Systems

<sup>1</sup>CPS are engineered systems that are built from, and depend upon, the seamless integration of computational algorithms and physical components.

*Large scale interconnection – Compositional design tools*



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<sup>1</sup>[http://www.nsf.gov/funding/pgm\\\_summ.jsp?pims\\\_id=503286](http://www.nsf.gov/funding/pgm\_summ.jsp?pims\_id=503286)