

TRUST-BASED CONTROL, DECISION-MAKING, AND MOTION PLANNING FOR HUMAN-ROBOT COLLABORATION SYSTEMS

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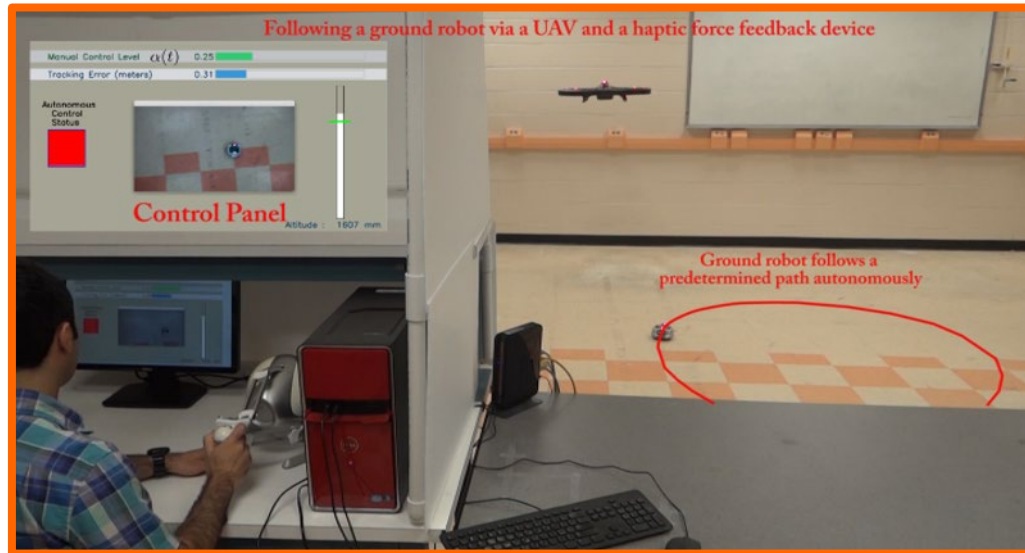
Control Systems and the Quest for Autonomy

A Symposium in Honor of Professor Panos J. Antsaklis

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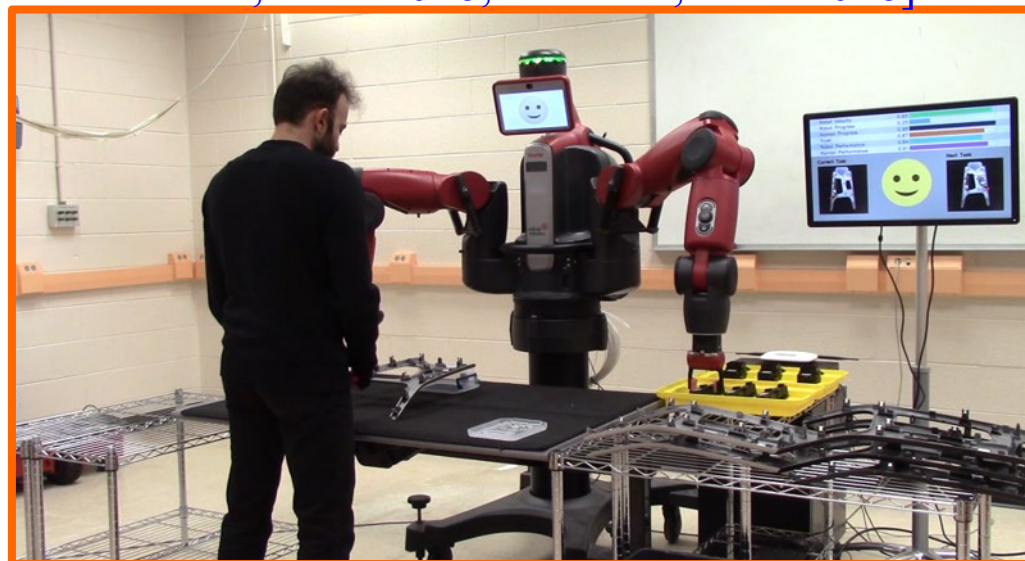
I2R Research Overview



[Fu et. al., JGCD 2018; Saeidi et. al., T-Ro 2017; Saeidi et. al., ACC 2016; Fu et. al., ACC 2016]



[Saeidi et. al., IROS 2017]



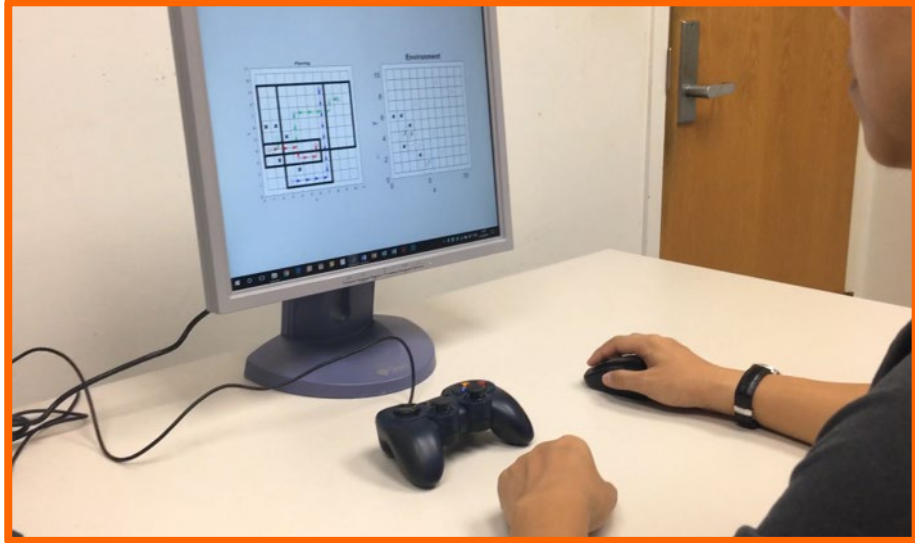
[Mizanoor & Wang, Mechatronics, 2018; Sadr & Wang, TASE 2017; Sadr et. al., CASE 2016]



[Jiang & Wang, CPHS 2018; Liao et. al., ACC 2017; Wang, TCST 2016; Wang, ACC 2016]

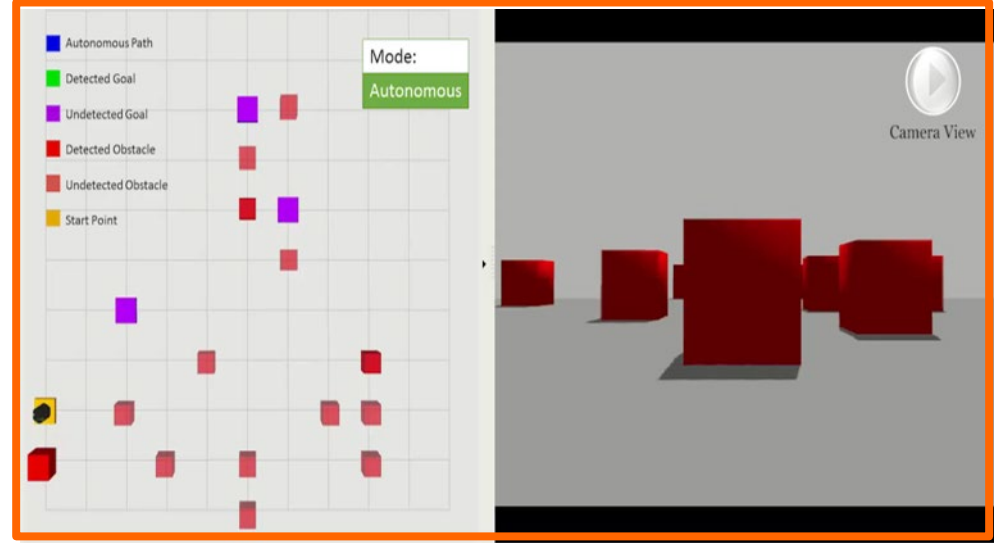
I2R Research Overview

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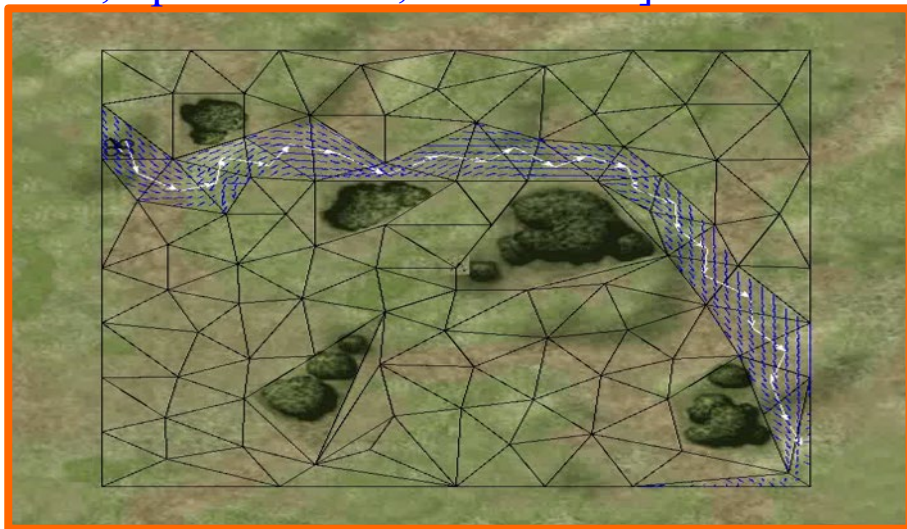
[Zheng et. al., DSCC 2018; Wang et. al., TiiS 2018; Spencer et. al., IROS 2016]

2

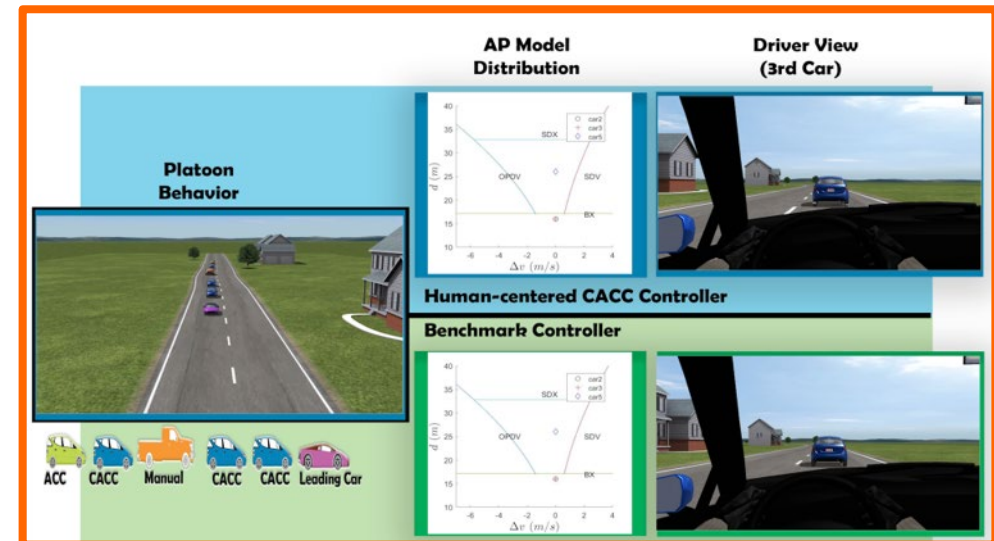


[Mahani & Wang, DSCC 2016]

3



[Mahani & Wang, DSCC 2018]



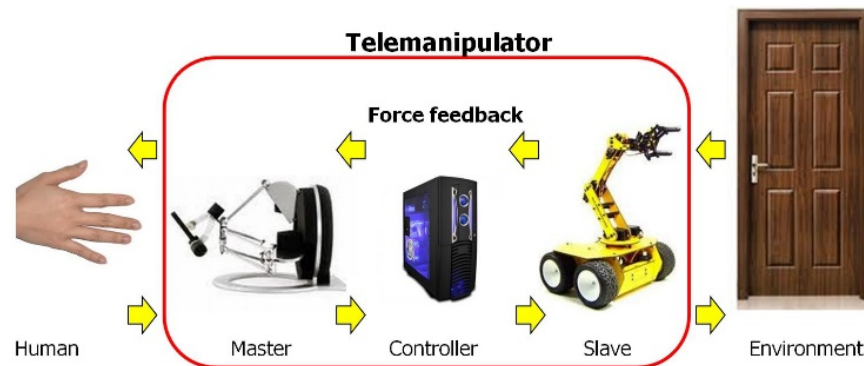
[Wang et. al., SAE WCX 2018; Li & Wang, T-ITS 2017; Dey et. al., T-ITS 2016; Wang & Wang, DSCC 2016]

Why is Trust Important?

- Adversarial, unpredictable, risky situations: Does a human trust autonomy to perform a task or prefer to do it by themselves? To what extent does the human trust autonomy?

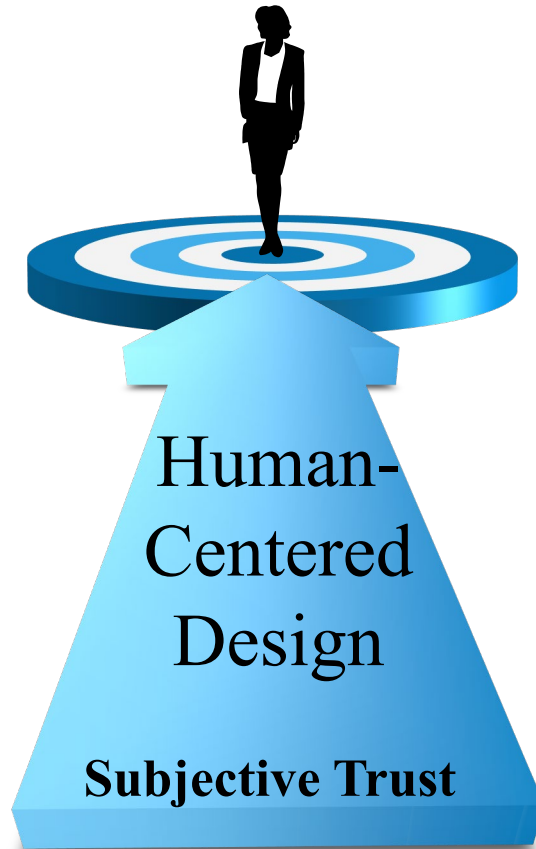


- Collaborative tasks: Human's acceptance and willingness work together with robots to achieve improved performance and balanced human experience.



Computational Trust Models

Our Trust Models



- Time-series trust model

[Wang et. al. Springer 2014; Sadrfaridpour et. al. Springer 2015; Rahman et. al. DSCC 2015a; Saeidi & Wang, CDC 2015; Saeidi et. al. ACC 2016; Sadrfaridpour et. al. CASE 2016; Rahman et. al. CASE 2016a; Spencer et. al., IROS 2016; Mahani & Wang, DSCC 2016; Saeidi et. al. T-Ro, 2017; Sadrfaridpour & Wang, TAES 2017]

- Dynamic Bayesian Network (DBN) trust model

[Wang et. al., ACM TiS, 2018]

- Robot-to-human trust model

[Walker et. al. MSCl 2015; Rahman et. al. CASE 2016a]

- Mutual trust model

[Wang et. al. ACC 2015, CPS 2015; Wang & Zhang ed., Spring 2017; Mizanoor & Wang, Mechatronics, 2018]

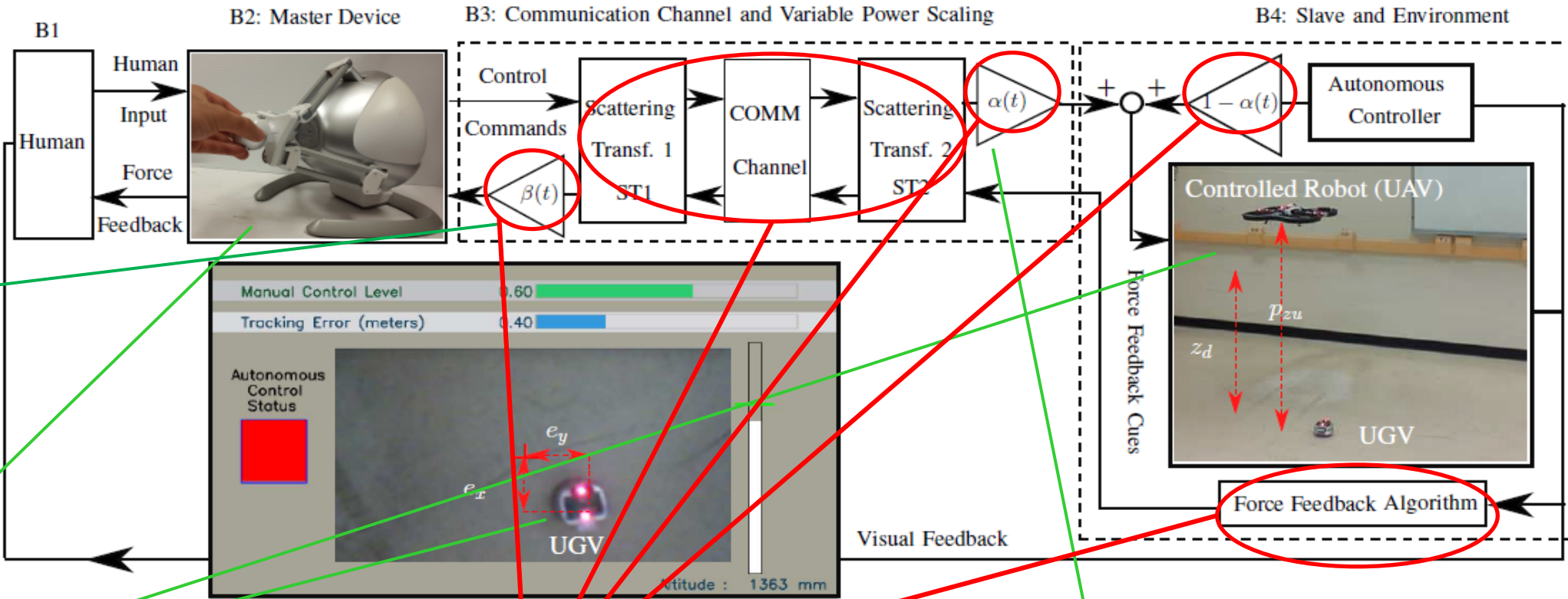
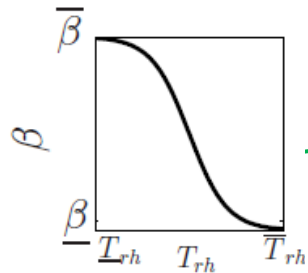
- RoboTrust for multi-robot systems

[Saeidi et. al., IROS 2017]

Mixed-Initiative Bilateral Haptic Teleoperation of Mobile Robots based on Mutual Trust Analysis

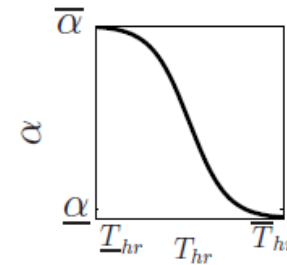
[Saeidi et. al, T-Ro 2017; Saeidi et. al. ACC 2016; Fu et. al., ACC 2016]

Function of robot-to-human trust

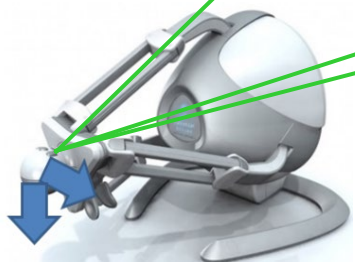


Possible sources of instability!

Passivity theory



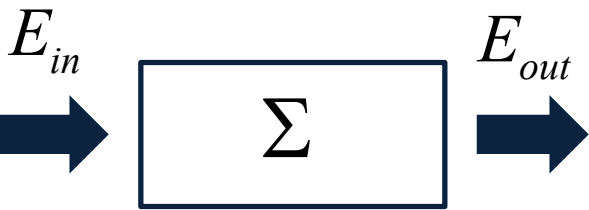
Function of human-to-robot trust



Mixed-Initiative Bilateral Haptic Teleoperation of Mobile Robots based on Mutual Trust Analysis

[Saeidi et. al. ACC 2016; IEEE T-Ro 2017; Fu et. al., ACC 2016]

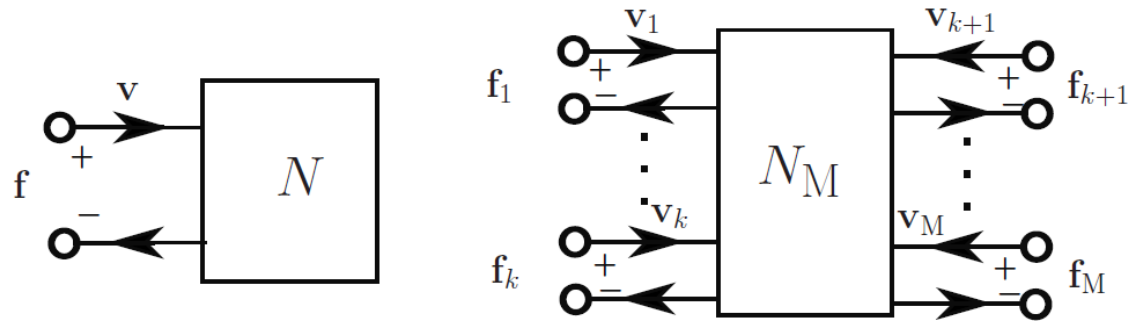
Passivity Theory & Port Network Theory



$$\Sigma : \dot{x} = f(x(t), u(t), t)$$

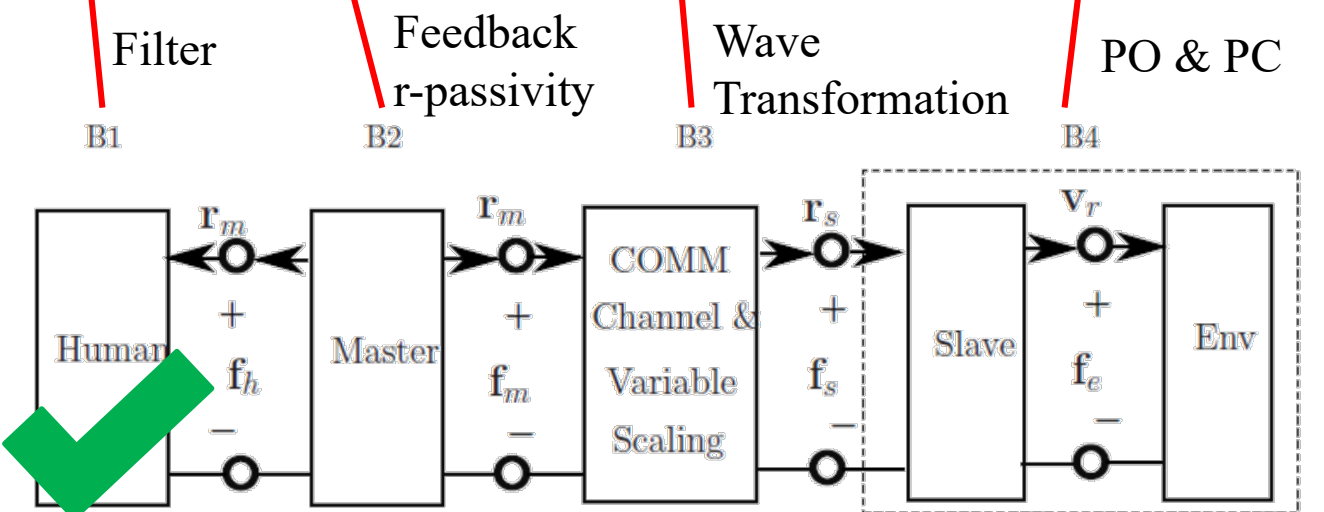
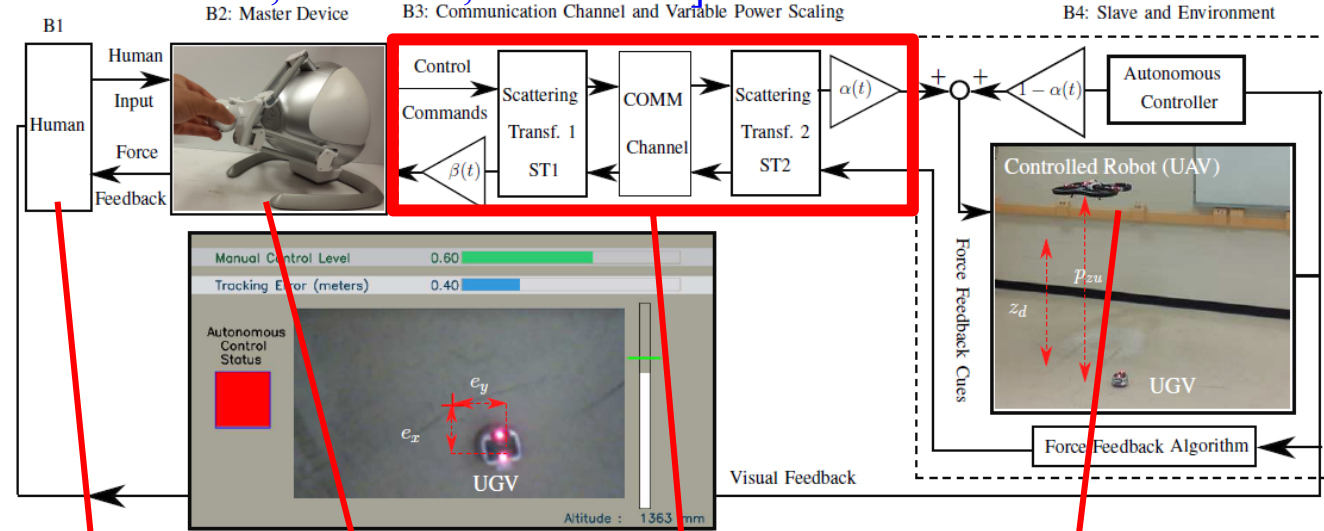
$$E_{out} \leq E_{in}$$

- Passive systems are stable
- Interconnection of passive n ports results in a larger passive system



$$\int_0^t \mathbf{I}^T(\tau) \mathbf{O}(\tau) d\tau + E(0) \geq 0 \text{ must hold for } \mathbf{I}^T(t) \mathbf{O}(t) \triangleq \mathbf{v}_1^T(t) \mathbf{f}_1(t) + \dots + \mathbf{v}_M^T(t) \mathbf{f}_M(t)$$

In teleoperation, force and velocity commands form the power ports



Port-based model for the mixed-initiative bilateral haptic teleoperation

Mixed-Initiative Bilateral Haptic Teleoperation of Mobile Robots based on Mutual Trust Analysis

[Saeidi et. al. ACC 2016; IEEE T-Ro 2017; Fu et. al., ACC 2016]

Master

Dynamics of Master Haptic Device

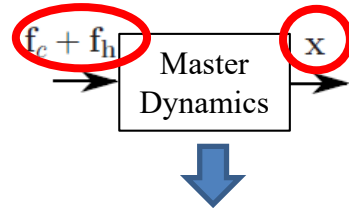
$$M(\mathbf{x})\ddot{\mathbf{x}} + C(\mathbf{x}, \dot{\mathbf{x}})\dot{\mathbf{x}} = \mathbf{f}_c + \mathbf{f}_h \quad \mathbf{f}_c = -\mathbf{f}_{\text{local}} - \mathbf{f}_m$$

$$\mathbf{f}_{\text{local}} = B\dot{\mathbf{x}} + K\mathbf{x},$$

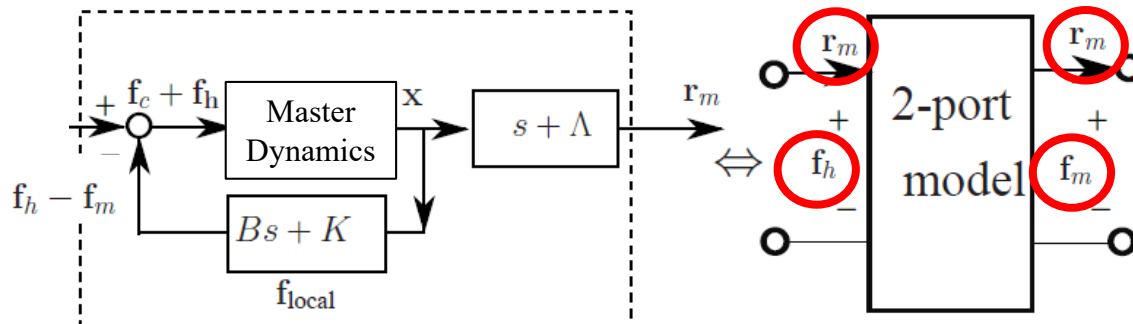
$$B = \text{diag}[b_1, \dots, b_n] \in \mathbb{R}^{n \times n}, b_j > 0, j = 1, \dots, n,$$

$$K = \text{diag}[k_1, \dots, k_q, 0, \dots, 0] \in \mathbb{R}^{n \times n},$$

$$k_i > 0, i = 1, \dots, q \leq n$$



Feedback r passive master



Comm. Channel

↓

Slave

Feedback r – Passivity of the Master

$$\mathbf{r}_m = \dot{\mathbf{x}} + \Lambda\mathbf{x}$$

$$\Lambda = \text{diag}[\lambda_1, \lambda_2, \dots, \lambda_q, 0, \dots, 0] \in \mathbb{R}^{n \times n} \text{ with } \lambda_i > 0$$

$$V_{hd}(t) := \frac{1}{2} [\mathbf{r}_m^T M \mathbf{r}_m + \mathbf{x}^T (K + \Lambda B - \Lambda M \Lambda) \mathbf{x}] \geq 0$$

$$S_{hd}(t) := \dot{\mathbf{x}}^T [B - \frac{1}{2}(M\Lambda + \Lambda M)] \dot{\mathbf{x}} + \mathbf{x}^T \Lambda K \mathbf{x} - \mathbf{x}^T \Lambda C \dot{\mathbf{x}} \geq 0,$$

$$\mathbf{r}_m^T(t) (\mathbf{f}_h(t) - \mathbf{f}_m(t)) = \dot{V}_{hd}(t) + S_{hd}(t)$$

$$\int_0^t \mathbf{r}_m^T(\tau) (\mathbf{f}_h(\tau) - \mathbf{f}_m(\tau)) d\tau = V_{hd}(t) - V_{hd}(0)$$

Passivity inequality

$$+ \int_0^t S_{hd}(\tau) d\tau \geq -V_{hd}(0).$$

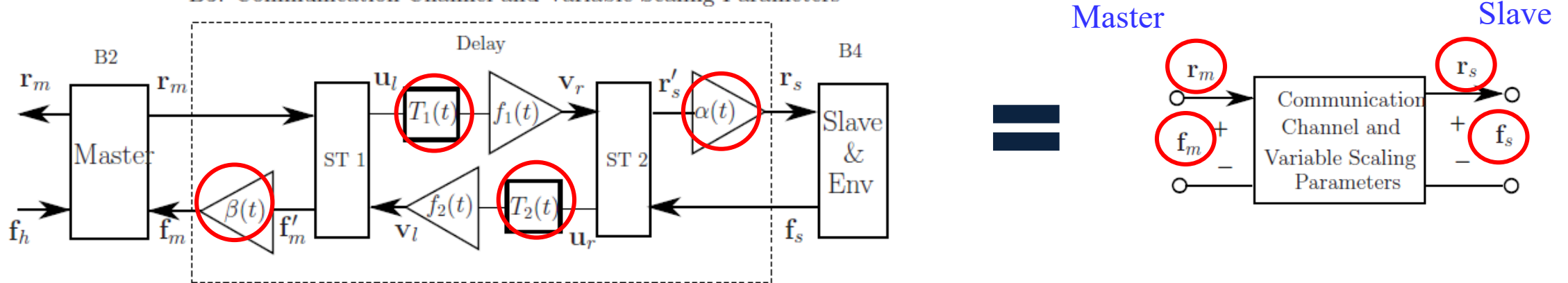
Mixed-Initiative Bilateral Haptic Teleoperation of Mobile Robots based on Mutual Trust Analysis

[Saeidi et. al. ACC 2016; IEEE T-Ro 2017; Fu et. al., ACC 2016]

Passivity of the Communication Channel with Variable Time-Delay & Variable Scaling

Block diagram for the communication channel with time-varying delays and variable power scaling

B3: Communication Channel and Variable Scaling Parameters



Scattering/wave transformation

$$\mathbf{u}_l = \sqrt{\frac{\beta}{2b}}(\mathbf{f}'_m + b\mathbf{r}_m), \quad \mathbf{v}_l = \sqrt{\frac{\beta}{2b}}(\mathbf{f}'_m - b\mathbf{r}_m), \quad \mathbf{u}_r = \sqrt{\frac{\alpha}{2b}}(\mathbf{f}_s - b\mathbf{r}'_s), \quad \mathbf{v}_r = \sqrt{\frac{\alpha}{2b}}(\mathbf{f}_s + b\mathbf{r}'_s)$$

$$\underline{f_i = \sqrt{1 - \dot{T}_{i \max}}, \quad i = 1, 2, \quad b > 0: \text{Characteristic impedance}}$$

$$\frac{dT_i}{dt} \leq \dot{T}_{i \max} \leq 1, \quad i = 1, 2$$

$\dot{T}_{i \max}$: The maximum rate of increase of time-varying delay $T_i(t)$

Passivity inequality

$$\int_0^t \mathbf{r}_m^T(\tau)\mathbf{f}_m(\tau) - \mathbf{r}_s^T(\tau)\mathbf{f}_s(\tau)d\tau \geq 0 \text{ assuming } E(0) = 0$$

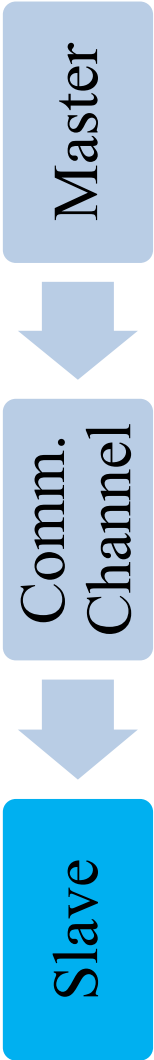
Master

Comm. Channel

Slave

Mixed-Initiative Bilateral Haptic Teleoperation of Mobile Robots based on Mutual Trust Analysis

[Saeidi et. al. ACC 2016; IEEE T-Ro 2017; Fu et. al., ACC 2016]



Passivity of the Slave using PO & PC

Passivity observer (PO):

An energy observer function

$$E_{obs}(t) = \int_0^{t^-} \mathbf{r}_s^T(\tau) \mathbf{f}_s(\tau) d\tau$$

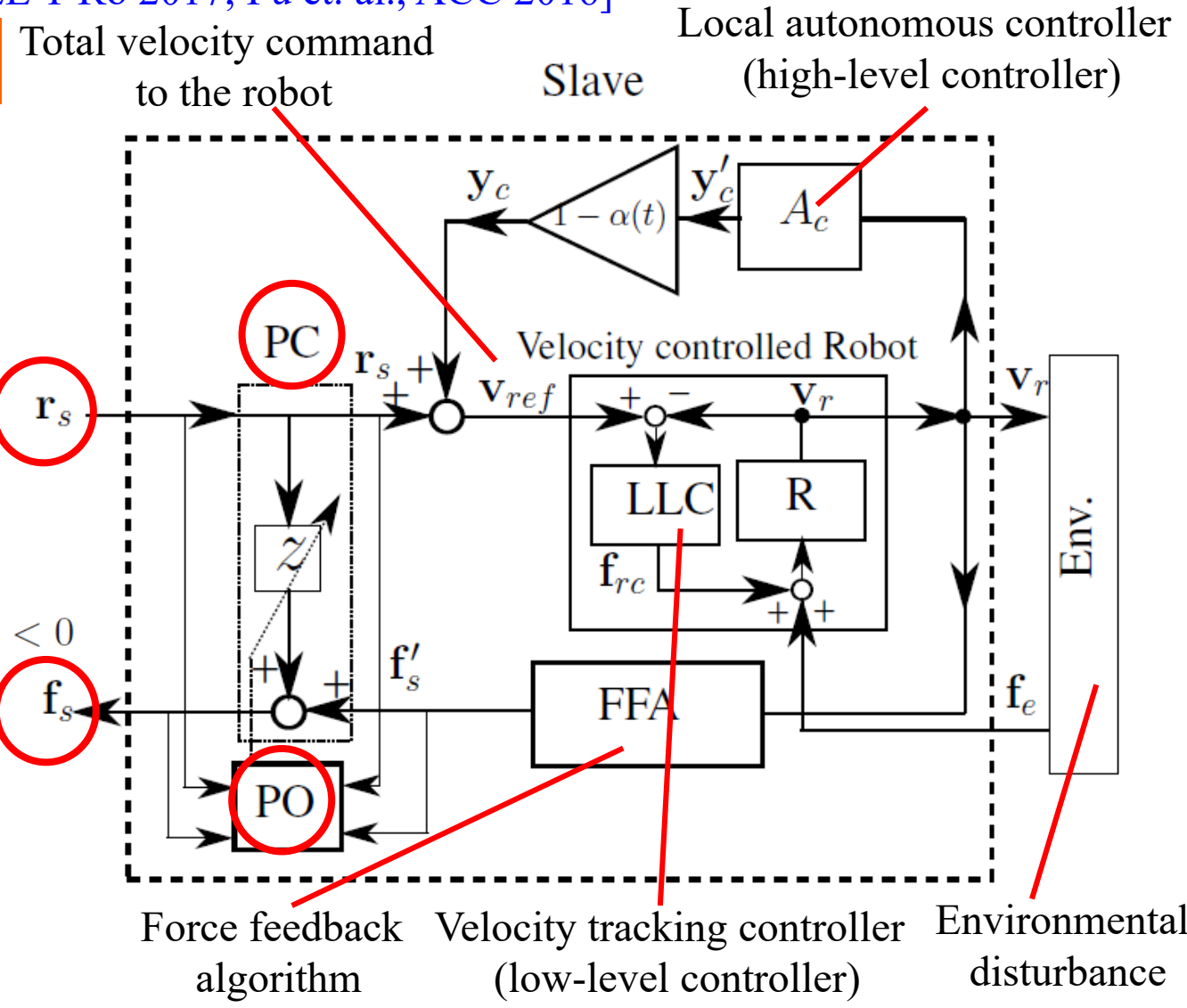
Passivity controller (PC):

a time-varying dissipation activation function

$$z(t) = \begin{cases} -\frac{\mathbf{r}_s^T(t) \mathbf{f}'_s(t)}{\|\mathbf{r}_s(t)\|_2^2} & \text{if } E_{obs}(t) = 0 \text{ \& } \mathbf{r}_s^T(t) \mathbf{f}'_s(t) < 0 \\ 0 & \text{otherwise} \end{cases}$$

$$\mathbf{f}_s(t) = \mathbf{f}'_s(t) + z(t) \mathbf{r}_s(t)$$

Passivity of the slave $\int_0^t \mathbf{r}_s^T(\tau) \mathbf{f}_s(\tau) d\tau \geq 0$





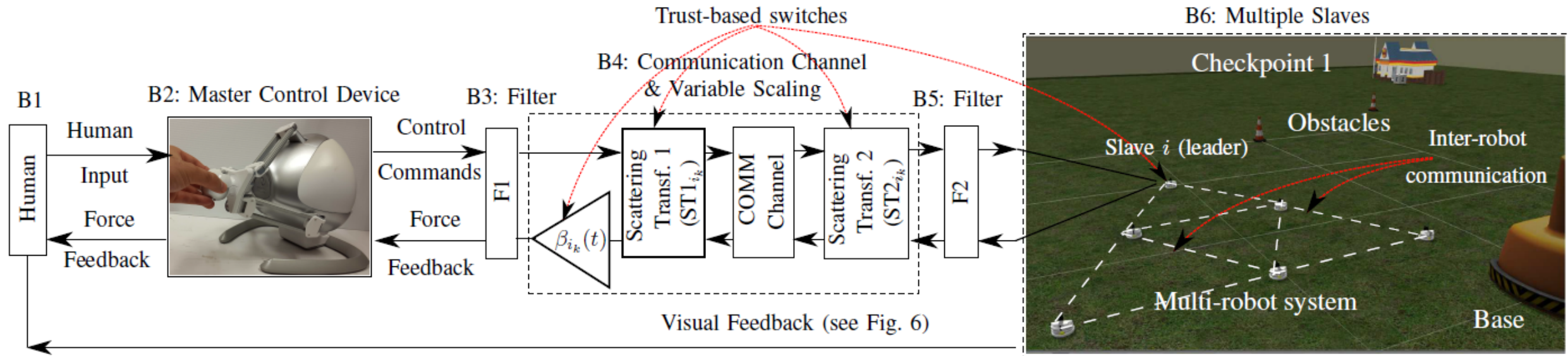
A Mixed-Initiative Haptic Teleoperation Strategy for Mobile Robotic Systems Based on Bidirectional Computational Trust Analysis

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Clemson University**



Trust-Based Leader Selection for Bilateral Haptic Teleoperation of Multi-Robot Systems

[Saeidi et. al. IROS 2017]



- Multi-robot collective position tracking and synchronization
- RoboTrust:
 - Human-to-robot trust: dynamic criterion to select leader → improved performance
 - Robot-to-human trust: dynamically scale the haptic force feedback → reduced workload
- Passivity approaches for switched systems

Trust-Based Leader Selection for Bilateral Haptic Teleoperation of Multi-Robot Systems

[Saeidi et. al. IROS 2017]

Robot Dynamics

$$\dot{\mathbf{p}}_i(t) = \mathbf{v}_i(t), \text{ for } i = \{1, 2, \dots, N\}$$

$$\mathbf{v}_l(t) = r_{s_k}(t), \text{ for leader } i = l$$

$$\mathbf{v}_i(t) = - \sum_{j \in \mathcal{N}_i \setminus l} a_{ij}(\mathbf{p}_i - \mathbf{p}_j) - a_{il}(\mathbf{p}_i - \mathbf{p}_l), \quad \forall i \neq l,$$

$$\dot{\mathbf{p}}_l(t) = r_{s_k}(t)$$

$$\dot{\mathbf{p}}_f(t) = -L_f \mathbf{p}_f(t) - A_f(\mathbf{p}_f(t) - \mathbf{1}p_l(t)),$$

Error Dynamics

$$\tilde{\mathbf{p}}_f(t) = \mathbf{p}_f(t) - \mathbf{1}p_l(t), \quad \tilde{\mathbf{v}}_f(t) = \dot{\mathbf{p}}_f(t) - \mathbf{1}\dot{p}_l(t)$$

$$M_f = L_f + A_f \quad \text{position synchronization}$$

$$\dot{\tilde{\mathbf{p}}}_f = \dot{\mathbf{p}}_f(t) - \mathbf{1}\dot{p}_l(t) = -M_f \tilde{\mathbf{p}}_f(t) - \mathbf{1}\dot{r}_{s_k}(t)$$

$$\dot{\tilde{\mathbf{v}}}_f = -M_f \tilde{\mathbf{v}}_f(t) - \mathbf{1}\dot{r}_{s_k}(t) \quad \text{velocity synchronization}$$

Performance Improvement Analysis

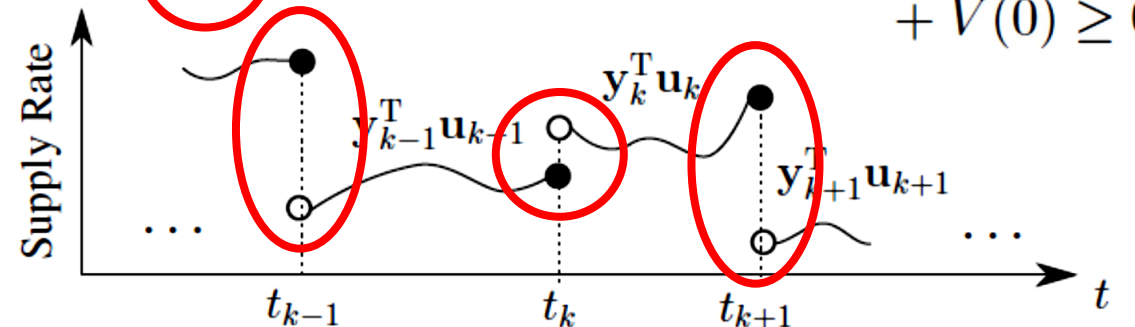
$$P_{r_i}(t) = -\tilde{\mathbf{p}}_f^T(t) \dot{\tilde{\mathbf{p}}}_f(t), \quad P_{r_i}(t) = -\tilde{\mathbf{v}}_f^T(t) \dot{\tilde{\mathbf{v}}}_f(t)$$

$$\tilde{\mathbf{p}}_f^T(t) \dot{\tilde{\mathbf{p}}}_f < 0 \quad \tilde{\mathbf{v}}_f^T(t) \dot{\tilde{\mathbf{v}}}_f < 0$$

Passivity Def. for Switched I/Os

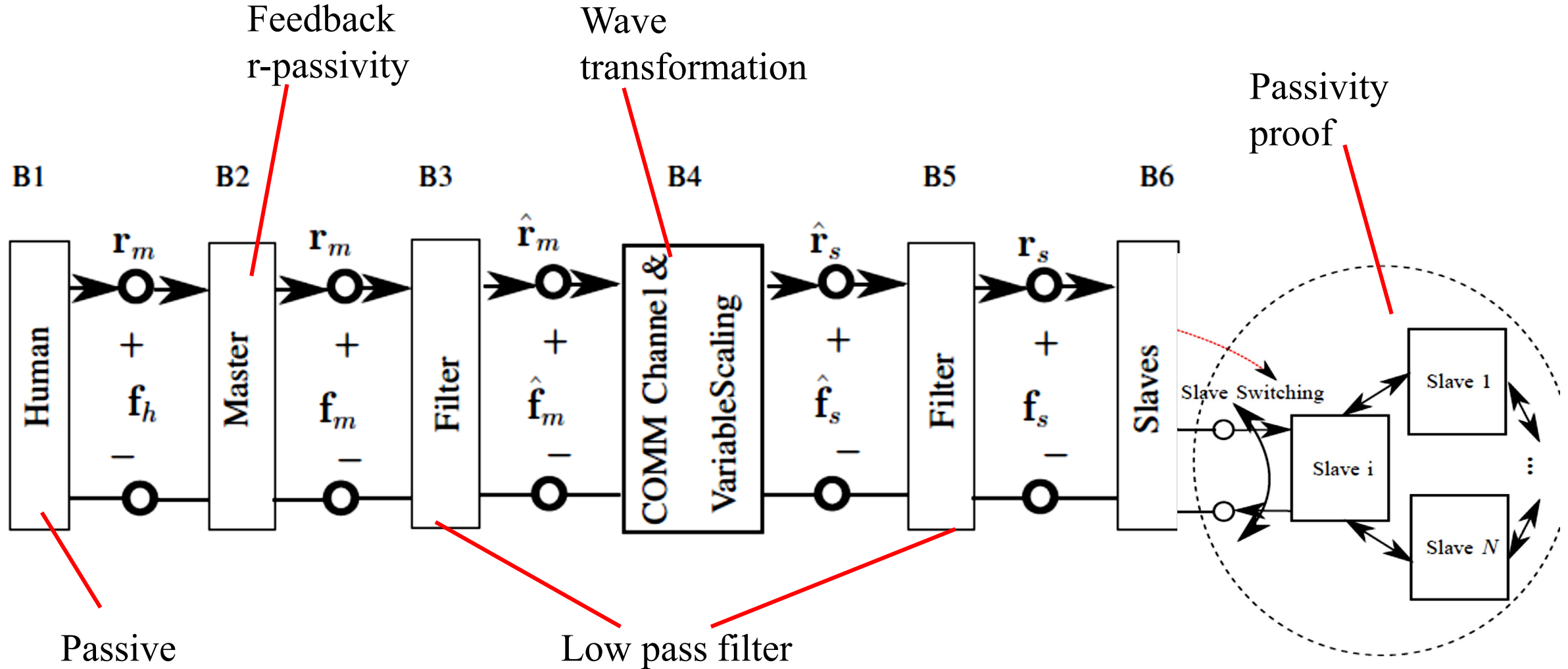
Definition 1: A system Z with discontinuous supply rate, and/or switched inputs/outputs with a common storage function is passive if the following holds [12]

$$\sum_{k=0}^{S-1} \left\{ \int_{t_k^+}^{t_{k+1}} \mathbf{y}_k^T(\tau) \mathbf{u}_k(\tau) d\tau \right\} + \int_{t_S^+}^t \mathbf{y}_S^T(\tau) \mathbf{u}_S(\tau) d\tau + V(0) \geq 0$$



Trust-Based Leader Selection for Bilateral Haptic Teleoperation of Multi-Robot Systems

[Saeidi et. al. IROS 2017]



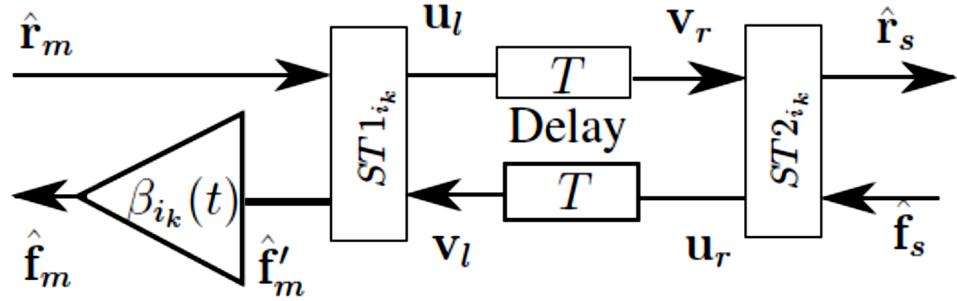
Port-based model for the bilateral haptic teleoperation of a multi-robot system

Trust-Based Leader Selection for Bilateral Haptic Teleoperation of Multi-Robot Systems

[Saeidi et. al. IROS 2017]

Passivity Definition & Wave Variable Transformation

$$\sum_{k=0}^{S-1} \left\{ \int_{t_k^+}^{t_{k+1}} \left(\hat{\mathbf{r}}_{m_k}^T(\tau) \hat{\mathbf{f}}_{m_k}(\tau) - \hat{\mathbf{r}}_{s_k}^T(\tau) \hat{\mathbf{f}}_{s_k}(\tau) \right) d\tau \right\} + \int_{t_S^+}^t \left(\hat{\mathbf{r}}_{m_S}^T(\tau) \hat{\mathbf{f}}_{m_S}(\tau) - \hat{\mathbf{r}}_{s_S}^T(\tau) \hat{\mathbf{f}}_{s_S}(\tau) \right) d\tau \geq 0.$$



$$\mathbf{v}_r = \sqrt{\frac{1}{2b_{i_k}}} (\hat{\mathbf{f}}_{s_k} + b_{i_k} \hat{\mathbf{r}}_{s_k}), \quad \mathbf{v}_l = \sqrt{\frac{\bar{\beta}_{i_k}}{2b_{i_k}}} (\hat{\mathbf{f}}'_{m_k} - b_{i_k} \hat{\mathbf{r}}_{m_k}),$$

$$\mathbf{u}_r = \sqrt{\frac{1}{2b_{i_k}}} (\hat{\mathbf{f}}_{s_k} - b_{i_k} \hat{\mathbf{r}}_{s_k}), \quad \mathbf{u}_l = \sqrt{\frac{\beta_{i_k}}{2b_{i_k}}} (\hat{\mathbf{f}}'_{m_k} + b_{i_k} \hat{\mathbf{r}}_{m_k})$$

Proof of Passivity

$$\hat{\mathbf{r}}_{m_k}^T(t) \beta_{i_k}(t) \hat{\mathbf{f}}'_{m_k}(t) = \frac{\beta_{i_k}(t)}{2} \left[\frac{\mathbf{u}_l^T(t) \mathbf{u}_l(t)}{\underline{\beta}_{i_k}} - \frac{\mathbf{v}_l^T(t) \mathbf{v}_l(t)}{\bar{\beta}_{i_k}} \right]$$

$$\hat{\mathbf{r}}_{s_k}^T(t) \hat{\mathbf{f}}_{s_k}(t) = \frac{1}{2} [\mathbf{v}_r^T(t) \mathbf{v}_r(t) - \mathbf{u}_r^T(t) \mathbf{u}_r(t)]$$

$$\sum_{k=0}^{S-1} \left[\int_{t_k^+}^{t_{k+1}} \left(\hat{\mathbf{r}}_{m_k}^T(\tau) \hat{\mathbf{f}}_{m_k}(\tau) - \hat{\mathbf{r}}_{s_k}^T(\tau) \hat{\mathbf{f}}_{s_k}(\tau) \right) d\tau \right] \geq \frac{1}{2} \left[\int_{t_S-T}^{t_S} \mathbf{u}_l^T(\tau) \mathbf{u}_l(\tau) d\tau + \int_{t_S-T}^{t_S} \mathbf{u}_r^T(\tau) \mathbf{u}_r(\tau) d\tau \right]$$

$$\int_{t_S^+}^t \left(\hat{\mathbf{r}}_{m_S}^T(\tau) \hat{\mathbf{f}}_{m_S}(\tau) - \hat{\mathbf{r}}_{s_S}^T(\tau) \hat{\mathbf{f}}_{s_S}(\tau) \right) d\tau$$

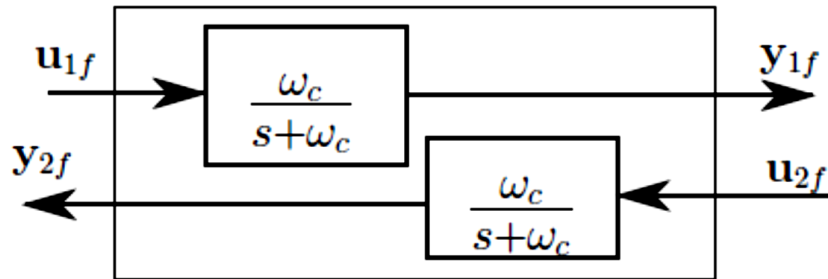
⋮

$$\geq \frac{1}{2} \left[\int_{t-T}^t \mathbf{u}_l^T(\tau) \mathbf{u}_l(\tau) d\tau + \int_{t-T}^t \mathbf{u}_r^T(\tau) \mathbf{u}_r(\tau) d\tau \right] \geq 0$$

Trust-Based Leader Selection for Bilateral Haptic Teleoperation of Multi-Robot Systems

[Saeidi et. al. IROS 2017]

Passive Filtering



Two-port filter.

$$\mathbf{y}_k^T(t) \mathbf{u}_k(t) \triangleq$$

$$\mathbf{u}_{1f_k}^T(t) \mathbf{y}_{2f_k}(t) - \mathbf{u}_{2f_k}^T(t) \mathbf{y}_{1f_k}(t) = 0.$$

The relative position of the leader robot with its neighbors as haptic feedback

Passivity of the Slave Side

$$\dot{\mathbf{p}}(t) = (\Omega(t) - I)L\mathbf{p}(t) + D_{i_k}(t)r_{s_k}(t)$$

$$\Omega(t) = \text{diag}[D(t)]$$

$$D_{i_k}(t) = [\delta_{1_k}(t) \cdots \delta_{N_k}(t)]^T \in R^{N \times 1}$$

$$\delta_{i_k}(t) = \begin{cases} 1 & \text{if slave } i \text{ is the leader} \\ 0 & \text{otherwise} \end{cases}$$

The multi-robot system is passive with

$$V_{f_s}(t) = \frac{1}{2} \mathbf{p}^T(t) L \mathbf{p}(t) \geq 0$$

input $r_{s_k}(t)$

output $f_{s_k}(t) = D_{i_k}(t)^T L \mathbf{p}(t)$



Trust-Based Leader Selection for Bilateral Haptic Teleoperation of Multi-Robot Systems

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Department of Mechanical Engineering
Clemson University**



Thank You!

Students, Postdocs, & Alumni



Dr. Hamed Saeidi



Dr. Rahman Mizanoor



Dr. Behzad Sadr



Mr. Adam Spencer



Mr. Xiaotian Wang



Mr. Zhanrui Liao



Ms. Qiuchen Wang



Mr. Foster McLane



Mr. Longsheng Jiang



Mr. Maziar Mahani



Mr. Fangjian Li



Mr. Huanfei Zheng



Mr. Jonathan Todd



Mr. James Svacha