# **Terahertz laser frequency combs**

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Terahertz light can be used to identify numerous complex molecules, but has traditionally remained unexploited due to the lack of powerful broadband sources. Pulsed lasers can be used to generate broadband radiation, but such sources are bulky and produce only microwatts of average power. Conversely, although terahertz quantum cascade lasers are compact semiconductor sources of high-power terahertz radiation, their narrowband emission makes them unsuitable for complex spectroscopy. In this work, we demonstrate frequency combs based on terahertz quantum cascade lasers, which combine the high power of lasers with the broadband capabilities of pulsed sources. By fully exploiting the quantum-mechanically broadened gain spectrum available to these lasers, we can generate 5 mW of terahertz power spread across 70 laser lines. This radiation is sufficiently powerful to be detected by Schottky-diode mixers, and will lead to compact terahertz spectrometers.

ptical frequency combs<sup>1</sup> have revolutionized high-precision metrology and spectroscopy<sup>2</sup>. At long-wavelength terahertz frequencies, combs generated by pulsed lasers<sup>3</sup> have proven to be useful sources of radiation for detecting molecular fingerprints, because many molecules have strong rotational and vibrational resonances in the terahertz regime<sup>4,5</sup>. However, these sources have difficulty achieving powers of more than a few microwatts, are typically detected coherently, and are bulky and involve expensive mode-locked lasers. Terahertz quantum cascade lasers<sup>6</sup> (THz QCLs), on the other hand, are powerful compact sources of such radiation and are capable of generating watt-level power output<sup>7</sup>. If they could be made to generate the uniformly spaced lines of a frequency comb, they would be ideal candidates for making compact spectrometers.

There are many ways to generate optical frequency combs, including intracavity phase modulation<sup>8</sup>, pumping microresonators with high-intensity radiation9, downconversion of a higher-frequency comb<sup>10</sup> and upconversion of a lower-frequency source<sup>11,12</sup>. However, the most powerful sources of frequency combs are generally mode-locked lasers, which in the time domain create a train of pulses and in the frequency domain create uniformly spaced lines. Mode-locked lasers can be classified into two varieties: actively mode-locked lasers, in which pulses are generated by an external modulation of the laser gain at the round-trip frequency, and passively mode-locked lasers, in which pulses generate their own modulation with the aid of saturable absorbers. Unfortunately, because external modulation is never as short as the pulse itself, actively mode-locked lasers cannot produce pulses as short as passively mode-locked lasers<sup>13</sup>. In the frequency domain, the spectral bandwidths of actively mode-locked lasers are therefore much narrower than those of passive ones.

In QCLs, mode-locking is difficult to achieve as the picosecond gain recovery time of the laser prevents stable pulse formation<sup>14</sup>. Although active mode-locking of mid-infrared QCLs<sup>15</sup> and THz QCLs<sup>16</sup> has been achieved, they were unable to exploit the full gain bandwidth available to the laser. On the other hand, recent work has demonstrated that when the group velocity dispersion

(GVD) of a mid-infrared QCL is made sufficiently low by using a broadband heterogeneous gain medium, such devices can passively form frequency combs based on four-wave mixing<sup>17</sup>. Although this mechanism does not produce time-domain pulses with high peak intensities, the frequency comb produced is suitable for linear applications such as dual-comb spectroscopy<sup>18,19</sup> and optical coherence tomography<sup>20</sup>. Using this approach, Hugi et al.<sup>17</sup> increased the bandwidth of mid-infrared QCL combs from the 15 cm<sup>-1</sup> achieved using active mode-locking to over 60 cm $^{-1}$  (at 7  $\mu$ m). However, a straightforward implementation of this approach is unlikely to work at terahertz frequencies, because terahertz electromagnetic waves strongly couple with the crystalline lattice and are thus orders of magnitude more dispersive than mid-infrared waves. Figure 1a shows the calculated GVD of GaAs at 40 K. At 3.5 THz, the GVD is  $87,400 \text{ fs}^2 \text{ mm}^{-1}$ , which is 250 times greater than the GVD at 7  $\mu$ m (320 fs<sup>2</sup> mm<sup>-1</sup>). Simply using a broadband gain medium is not sufficient to overcome the dispersion of the material itself and permit comb formation.

To overcome this problem, we integrated dispersion compensation into our waveguides to deliberately cancel the cavity dispersion. The basic idea, illustrated in Fig. 1b, is that a chirped corrugation is etched into the facet of the laser, the period of which tapers from short to long as its amplitude increases. Longwavelength waves (which have higher group velocities) travel to the end of the cavity before reflecting, while short-wavelength waves reflect earlier, thereby compensating dispersion. Essentially, this corrugation mimics the double-chirped mirrors used to generate octave-spanning spectra in the near-infrared and visible range<sup>21</sup>. To design such compensators, an accurate measurement of the dispersion of a real laser waveguide is essential. For this, terahertz timedomain spectroscopy<sup>22</sup> (THz TDS) was performed on single-section metal-metal waveguide lasers, using the biased QCL itself as a generator of time-domain pulses. Although this method is less accurate than two-section techniques for measuring laser gain<sup>23–25</sup>, it permits a cleaner measurement of the round-trip phase because the terahertz pulse does not encounter gaps that could distort the transmitted pulse. The inset of Fig. 1a shows the phase acquired by a

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## ARTICLES



**Figure 1 | GVD of laser gain medium. a**, Calculated GVD of GaAs at 40 K, defined here as  $D_2 \equiv \partial_{\omega}(1/v_g)$ . The marked frequencies are 3.5 THz and 42 THz. Inset: phase acquired by a time-domain terahertz pulse after travelling through a 775  $\mu$ m QCL twice, with a parabolic fit. **b**, Schematic of the integrated dispersion compensation scheme used. The longer-wavelength wave travels further before it reflects, while the shorter-wavelength wave reflects earlier, resulting in a shorter effective cavity.

pulse after travelling through a 775-µm-long laser twice; the highly nonlinear phase–frequency relation indicates a GVD of  $D_2 = 111,000 \text{ fs}^2 \text{ mm}^{-1}$ , which is substantially higher than what would be expected from GaAs alone. To account for uncertainties in the measurement and in device fabrication, seven different compensators were designed, which compensated the measured  $D_2$  adjusted by 0%,  $\pm 6.6\%, \pm 13.3\%$  and  $\pm 20\%$ . Details of the design parameters can be found in Supplementary Fig. 1.

Figure 2a shows the broad terahertz spectrum generated by a correctly GVD-compensated 5-mm-long QCL with a hyperhemispherical lens attached<sup>26</sup>. Because the gain medium—a homogeneous four-well resonant phonon design—has a strong injector anticrossing, the gain medium has two peaks, one near 3.3 THz and one near 3.8 THz (ref. 27). However, only the design overcompensated by +13.3% produces such a broad spectrum; the rest lase at only a few modes, indicating that it is essential to correctly compensate GVD for possible comb formation.

An interesting side effect of the broadband terahertz generation is that this same design—and only this design (Supplementary Fig. 1c)—generates a strong RF beat note at the round-trip frequency of the laser (~6.8 GHz) when d.c.-biased. Without taking into account RF losses from the bond wire, as much as -33 dBm of power has been observed leaking out of the 5 mm QCLs, as measured using a bias-tee. Although similar beat notes have previously been observed on the bias lines of metal–metal waveguides<sup>28</sup>, at -65 dBm they were three orders of magnitude weaker. This strong RF signal implies that the beat notes generated from all the pairs in the spectra are adding up coherently. Figure 2b shows the



**Figure 2** | Continuous-wave spectrum and beat notes. **a**, Spectrum of a THz QCL comb biased to 0.9 A at a temperature of 50 K. The device is 20  $\mu$ m wide, 5 mm long and emits 4.7 mW at 45 K. Atmospheric absorption is shown in grey. **b**, QCL-generated beat notes offset relative to 6.82 GHz, shown with the environmental fluctuations stabilized and unstabilized. (The spectra are discontinuous at 40 MHz because the signal below 40 MHz was measured by downconverting and sampling, while the signal above was measured with a spectrum analyser.) **c**, HEB-detected beat-note offset relative to 6.80 GHz, stabilized. The linewidth of 1.53 kHz is limited by the instrument resolution. **d**, Bias dependence of the beat-note frequency measured by the QCL and by the HEB. A repetition rate tuning of 12 MHz is possible, giving a total frequency shift of 6.80 GHz at 3.8 THz, approximately the mode spacing.

RF beat note emanating from such a laser, offset relative to a local oscillator at its repetition rate. Because the devices are mounted in a pulsed-tube cryocooler, mechanical vibrations cause the optical feedback to be unstable and impart low-frequency fluctuations on the beat note. By slowly applying a sub-milliamp modulation to the bias of the laser (Supplementary Fig. 2), we remove 99.92% of its free-running phase noise and stabilize its output. No major sidebands are visible other than the one at 350 kHz created by the phase-locked loop.

We now show that the beat-note-producing devices indeed possess the uniformly spaced lines of a frequency comb. A straight-forward way to test this is to shine the laser light onto a fast detector and to examine the resulting optical beating between all the laser modes. If only one narrow beat note were observed, that would indicate that all of the detected modes were evenly spaced. Conversely, a non-comb would have multiple beat notes; for example, two frequencies separated by 500 GHz would have mode spacings differing by hundreds of megahertz. For this measurement we used a superconducting NbN hot-electron bolometer mixer (HEB), because of its extreme sensitivity<sup>29</sup> and response beyond 7 GHz (ref. 30). Figure 2c shows a stabilized beat note measured



**Figure 3** | **Results of SWIFT measurement. a**, Normal interferogram and homodyne interferograms, as measured by the HEB. The normal interferogram represents a d.c. measurement, while the homodyne interferogram represents an RF measurement. The QCL is biased to 0.9 A and is at 50 K. Inset: zoomed-in view near the zero-path delay. **b**, Blue line: SWIFT correlation spectrum (calculated from homodyne interferograms). Red line: spectrum product (calculated from normal interferogram). Even though they are fundamentally different measurements, their excellent agreement indicates that most of the spectral power is in the frequency comb.

with the HEB, and Fig. 2d compares its bias dependence to the beat note measured from the QCL using a bias-tee. The close agreement between the two frequencies shows that the beat note from the QCL well characterizes the beat note from the HEB. In addition, the narrow linewidth of the stabilized HEB beat note (under 2 Hz; Supplementary Fig. 2b) implies that the mutual phase coherence between all the detected modes persists for over  $1 \times 10^9$  round trips through the laser cavity<sup>31</sup>.

Of course, the existence of a narrow beat note on a fast detector and a broad spectrum does not prove that all of the modes observed in the spectrum are actually contributing to that beat note; it might be the case that a strong pair dominates the beat note. We stress that conventional spectroscopic techniques like Fourier-transform spectroscopy (FTS) cannot be used to determine the presence of a comb, because their resolution is limited by the physical travel of a mechanical delay element and can only measure spectra to a resolution of  $\sim$ 1 GHz. To truly show that all the modes in the spectrum are uniformly spaced, we use an interferometric technique that functions by examining the components of the RF beat note as a function of the delay of a Michelson interferometer. In this scheme, we lock the repetition rate of the QCL to a synthesizer at frequency  $\Delta \omega$  and use that as a local oscillator for the homodyne detection of two signals, an in-phase signal  $(S_{T}(\tau))$  and an in-quadrature signal  $(S_{\Omega}(\tau))$ . (Previous work has examined only the intensity of the RF beat note; here we also record its phase<sup>17</sup>.) The advantage of this technique is that the Fourier transforms of the homodyne interferograms can be used to directly infer the correlation of the

electric field of a light source with a frequency-shifted version of itself, by the relation

$$\langle E^*(\omega)E(\omega \pm \Delta \omega) \rangle = \frac{1}{2} (S_{\mathrm{I}}(\omega) \mp iS_{\mathrm{Q}}(\omega)) \equiv X_{\pm}(\omega)$$

where  $E(\omega)$  is the electric field of the source, angle brackets represent an average over laboratory timescales (in seconds) and a convolution with the instrument's apodization function,  $S_{\rm I}(\omega)$  and  $S_{\rm Q}(\omega)$ are the Fourier transforms of the measured homodyne interferograms, and  $X_{\pm}(\omega)$  are referred to as 'correlations'. We call this shifted wave interference Fourier-transform spectroscopy, or SWIFT spectroscopy for short. A normal Fourier-transform spectrum measures the d.c. component of the optical power through an interferometer, whereas a SWIFT spectrum measures its fastvarying components. (For more details, see Supplementary section 'SWIFT spectroscopy analysis'.)

There are some key differences between conventional FTS and SWIFT spectroscopy. For incoherent light sources, the SWIFT spectrum vanishes altogether, because the long-term phase incoherence between  $E(\omega)$  and  $E(\omega + \Delta \omega)$  causes their product to integrate to zero over laboratory timescales. Similarly, for a source consisting of two laser lines separated by  $\omega_1 - \omega_2 \neq \Delta \omega$ , the SWIFT spectrum is zero if  $\omega_1 - \omega_2 - \Delta \omega$  is larger than the integration bandwidth (Hz). In contrast, one may use a normal Fourier-transform spectrum to define a 'spectrum product' as  $X_{\rm sp}(\omega) \equiv \sqrt{\langle |E(\omega)|^2 \rangle \langle |E(\omega + \Delta \omega)|^2 \rangle}$  and while this product is superficially

### ARTICLES



**Figure 4** | **Bias dependence of beat-note and SWIFT spectra. a**, RF power measured from a bias-tee (amplified by 66 dB, with wiring losses of 20 dB) and terahertz power (calibrated) emitted by the QCL as a function of bias at 50 K, over the dynamic range of lasing operation. **b**, Linewidth of the RF signal emitted from the QCL as a function of bias, as measured with a spectrum analyser. (The linewidth metric used here is standard deviation.) The regions of stable comb formation are shaded and denoted I, II and III. **c**, SWIFT correlation spectra (measured with the HEB) and gain spectra (measured with THz TDS) corresponding to each of the three regions.

similar to  $|X_+(\omega)|$ , it will be non-zero as long as  $\omega_1 - \omega_2 - \Delta \omega$  is within the spectrometer's resolution (GHz). We can therefore compare  $|X_+(\omega)|$  and  $X_{\rm sp}(\omega)$  to reveal how comb-like a given laser spectrum is.

Figure 3a shows the SWIFT interferograms measured from a device biased to 0.9 A, together with a normal interferogram obtained at the same bias. Note that, although all three interferograms are nearly periodic with a spacing determined by the repetition rate of the laser, the SWIFT interferograms have non-zero phase and as a result are asymmetric about the zero path difference. In Fig. 3b we compare the correlation magnitude, calculated using SWIFT spectroscopy and the spectrum product, calculated using FTS. Their excellent agreement shows that essentially all of the laser's lines are separated by the repetition rate and we can truly call this a frequency comb. The correlation measurement shows approximately 70 comb lines above the noise floor, which span a total range of almost 500 GHz.

To see how the bias affects comb operation, we plot in Fig. 4a the optical and RF power generated by a QCL comb versus its bias in the range over which the device lases. At the onset of strong RF emission, there is a drop in total optical power that corresponds to the onset of comb formation. Similarly, Fig. 4b shows the linewidth of the QCL's RF emission versus bias. Not all biases within the range of strong RF emission actually form frequency combs, as there are certain biases at which the beat-note linewidth abruptly increases to several megahertz. Nonetheless, there are three distinct regions in which the beat-note linewidth is narrow and a stable comb is formed, denoted by regions I, II and III. To see whether we can actually exploit the full gain bandwidth at a given laser bias, we

compared the SWIFT spectra obtained in the three regions of comb formation with the gain spectra measured by terahertz time-domain spectroscopy, and plotted the result in Fig. 4c. In region I, the lower-frequency lobe experiences more gain and, as a result, the corresponding portion of the correlation spectrum dominates. In region II, the two lobes of the gain and correlation spectra are approximately equal in strength. In region III, the higherfrequency lobe is stronger and lases more strongly. This result demonstrates the effectiveness of the dispersion compensation technique, because it shows that frequency combs can be formed under various conditions with different gain profiles.

Finally, we beat our comb with a single-mode distributedfeedback (DFB) laser to investigate the absolute linewidth of each comb line. For this measurement, we shine the DFB laser directly into the facet of our comb laser and examine the heterodyne beating that is generated by the intracavity mixing<sup>32</sup> of the DFB laser and the comb laser. Although fast detectors like HEBs or Schottky mixers can be used to measure similar properties, this measurement also demonstrates one of the salient features of our comb: the ability to detect the frequency of terahertz lasers without any additional components (modulo the repetition rate). Figure 5a shows the spectra of the two lasers involved: a singlemode DFB laser at  $\sim$ 3.85 THz and the SWIFT spectrum of a comb biased near 0.9 A. Figure 5b shows the beat notes generated by our devices over a large frequency span. At a given bias, there are two lines present below the repetition rate, corresponding to beating of the DFB laser with the two nearest adjacent comb lines. Their frequencies therefore add up to the repetition rate of the comb. When the frequency of the DFB is shifted by shifting its

### ARTICLES



**Figure 5 | Heterodyne beat note between single-mode laser and comb. a**, Correlation spectrum of comb at 0.9 A (green) and spectrum of DFB laser (red). **b**, Heterodyne beating of free-running comb laser at 0.885 A with free-running DFB laser at various biases. The two lines correspond to beating between the two nearest comb lines and sum to the repetition rate of 6.8 GHz. The tuning coefficient of the DFB is 28 MHz mA<sup>-1</sup>. **c**, Zoomed-in view of one of the lines, showing a convolved FWHM of 2.5 MHz. From this, we estimate that our comb lines are 1.8 MHz wide.

bias, we observe that the two lines move in opposite directions by the laser's tuning coefficient (28 MHz mA<sup>-1</sup> in this case<sup>33</sup>). Even though the DFB laser is operating near the edge of the comb's bandwidth and only a few percent of the DFB's power can be coupled into the metal-metal waveguide, we are still able to measure beat notes with signal-to-noise ratios exceeding 10 dB. Figure 5c shows one of these beat notes over a smaller frequency span. Because the DFB's frequency and comb's offset frequency are both unstabilized, the measured full-width at half-maximum (FWHM) linewidth of 2.5 MHz represents a convolution between their respective lineshapes. Assuming they are identical Gaussians, we can infer an absolute comb linewidth of 1.8 MHz. Previous characterization of similar DFB lasers has measured free-running linewidths between 1 and 3 MHz (ref. 34), showing that our comb's offset frequency is as stable as a single-mode laser. Such linewidths are more than suitable for dual-comb spectroscopy at these wavelengths, due to the large ratio of the laser's repetition rate to its frequency.

In conclusion, we have demonstrated that THz QCLs can be used to generate high-power, broadband frequency combs. By applying dispersion compensation techniques from visible wavelengths to the THz QCL, we have shown that an arbitrary gain medium can be made to produce passive combs. Such combs cover a frequency range of almost 500 GHz with more than 70 lines at 3.5 THz and represent nearly an order of magnitude improvement over the ten modes obtained by active mode-locking<sup>16</sup>. The comb's bandwidth covers 14% of its centre frequency-the highest fractional bandwidth of integrated semiconductor frequency combs to datesuggesting that similar techniques can be used to improve Kerr-like combs at other wavelengths, including the mid-infrared. We have demonstrated SWIFT spectroscopy, a coherent detection scheme that can be used in combination with FTS to quantitatively measure the performance of such lasers and to measure the efficacy of comb formation. We have also demonstrated that, by utilizing intracavity mixing, these lasers can be used to compactly measure the frequency of single-mode lasers without the need for a highspeed terahertz detector or an external solid-state laser. To be truly useful for compact sensing applications, however, further

development is still required. At present, the gain medium's double-peaked shape causes the laser's energy to be split across two lobes and limits its general applicability, as the region between the two lobes experiences too much loss and cannot be accessed without a high-dynamic range detector. In addition, the weak interaction between the two lobes leads to a complicated bias dependence of the comb's properties and reduces its robustness. Fortunately, both of these issues are straightforward to resolve, as continuing development of heterogeneous gain media<sup>35</sup> will lead to flatter, broader comb spectra. Once octave-spanning spectra can be achieved, it may even be possible to stabilize the comb's absolute frequency<sup>36,37</sup> without any additional components, because the intracavity mixing process we demonstrated should also be capable of generating f-2f beating. Such combs could be used to form compact solid-state dual-comb spectrometers, which by utilizing intracavity mixing may even be able to operate without external detectors.

#### Methods

**Terahertz time-domain spectroscopy.** Dispersion and gain measurements were performed using a 775-µm-long, 30-µm-wide Fabry–Pérot QCL made from the same gain medium as the frequency comb devices, FL183S (wafer VB0481). Near-infrared pulses from a Ti:sapphire laser (80 fs, 25 mW) were shone into the facet of a biased laser, and the resulting terahertz pulses were used to characterize it. The first pulse that exits has passed through the waveguide once, whereas the second pulse has passed through three times. The amplitude ratio gives the gain, while the phase difference gives the dispersion. A silicon hyperhemispherical lens was attached to the output facet and electro-optic sampling<sup>38</sup> was used to sample the waveform, using a 300 µm [110] GaP wafer bonded to three 400 µm [100] GaP wafers.

**Homodyne interferometry (SWIFT spectroscopy).** Light from the lens-coupled THz QCL comb was collimated by an f/2 off-axis parabolic mirror (OAP), attenuated by a factor of 40 using a screen to prevent HEB saturation and passed through an optical chopper. It was then passed through a custom-built nitrogen-purged FTS that utilizes roof mirrors to minimize retroreflection into the QCL, and uses 1 mm of high-resistivity silicon as a beam splitter. Finally, light was focused onto the HEB using an f/3 OAP. The HEB was biased to 1 mV using a custom bias box and the current monitor was passed into a lock-in amplifier for the normal interferogram. The RF port of the HEB's bias-tee was amplified with a cryogenic low-noise amplifier (27 dB gain) and a room-temperature amplifier (31 dB gain). The RF signal was then downconverted and demodulated (Supplementary Fig. 2a) and the I and Q signals passed into lock-in amplifiers. All lock-ins used the same time constant of 1 ms, and the stage speeds used were 0.1 mm s<sup>-1</sup> (Fig. 3) and 0.3 mm s<sup>-1</sup> (Fig. 4). The FTS travel range was 10.75 cm, resulting in a resolution of 1.5 GHz.

**Heterodyne beat-note measurement.** For the heterodyne beating measurements of Fig. 5, a third-order DFB<sup>39,40</sup> was constructed using metal-metal waveguides fabricated from the same gain medium as the comb. It was 21  $\mu$ m wide, 450  $\mu$ m long and consisted of 15 periods of a corrugation that lased at 3.85 THz, with about a milliwatt of power. The DFB was operated in continuous-wave mode in a compact Stirling cryocooler at 47 K and its light was collimated using an *f*/3 OAP and focused onto the comb laser with an *f*/2 OAP. The RF beat notes were collected from the comb laser using a bias-tee and amplified with a low-noise amplifier providing 50 dB of gain. The resolution bandwidth for all heterodyne beat-note measurements was 3 MHz. The sweep times used in Fig. 5b,c were 31 ms and 51 ms, respectively.

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#### NATURE PHOTONICS DOI: 10.1038/NPHOTON.2014.85

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#### Author contributions

D.B. conceived the strategy, designed the devices, performed the measurements and completed the analysis. D.B. and N.H. performed electromagnetic simulations. T.-Y.K., N.H. and C.W.I.C. fabricated the devices. D.B., X.C. and Y.Y. performed the heterodyne beat-note measurements. D.J.H. and J.-R.G. provided the hot electron bolometer mixer. J.L.R. provided the material growth. All work was performed under the supervision of Q.H.

#### Additional information

Supplementary information is available in the online version of the paper. Reprints and permissions information is available online at www.nature.com/reprints. Correspondence and requests for materials should be addressed to D.B.

#### **Competing financial interests**

The authors declare no competing financial interests.