

MATH 10250 Practice Exam 1 - Extras

1. Factor: (a)  $x^2 + x - 2$       (b)  $x^2 - 9$

2. Write the **slope intercept form** of the equation of a line that passes through  $(-1, 4)$  and  $(2, 5)$

3. Given  $f(x) = \begin{cases} \frac{x^2 - 2x + 1}{x - 1} & \text{if } x < 1 \\ 0 & \text{if } x \geq 1 \end{cases}$

Find

(a)  $\lim_{x \rightarrow 1^-} f(x) =$

(b)  $\lim_{x \rightarrow 1^+} f(x) =$

(c)  $\lim_{x \rightarrow 1} f(x) =$

(d)  $f(1) =$

Is  $f$  continuous at  $x = 1$ ? Justify your answer.

4. Let  $f(x) = x^2 - 4\sqrt{x}$ . Find the (instantaneous) rate of change of  $f$  at  $x = 4$ .

5. Find derivative of

(a)  $f(x) = \frac{1}{2}\sqrt{x} + x^2 - \sqrt{2}$

(b)  $g(x) = \frac{2}{x^2} - x^{-1} + \sqrt[5]{x}$

(c)  $h(x) = 2\sqrt{100 - x^2}$

6. Find the **second** derivative of

$$f(x) = (x^3 - 3)^{-1}$$

7. Given

$$f(x) = \frac{\sqrt{2x}}{x^2 - 1}$$

What is  $f'(2)$ ?

8. The demand for VR-glasses is modeled by the function

$$p(x) = -x^2 - 4x + 64$$

where  $p$  is measured in dollars and  $x$  is measured in thousands of glasses.

1. Find the average rate of change in the unit price of VR-glasses if the quantity demanded is between 0 and 5 thousand.
2. What is the instantaneous change in the unit price of VR-glasses at a demand of 3 thousand units ( $x = 3$ )?

9. Given  $f(x) = \sqrt{2x}$  and  $g(x) = x^2 - x$ . Compute the following (Simplify your answers if possible; but, don't combine anything in part (a)):

(a)  $(f + g)(x) =$

(a)  $(f - g)(x) =$

(b)  $(fg)(x) =$

(c)  $\left(\frac{f}{g}\right)(x) =$

(e)  $(f \circ g)(x) =$

(f)  $(g \circ f)(x) =$

(g)  $(g \circ f)(2) =$