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%
% FIXED-POINT ALGORITHM 2.2
%
% To find a solution to  $p = g(p)$  given an
% initial approximation  $p_0$  (and the function  $g$ )
%
% This code solve Illustration problem on Page 60 of the textbook.
% formulation (d) is used
%
% INPUT:   initial approximation  $p_0$ ; tolerance TOL;
%          maximum number of iterations NI.
%
% OUTPUT:  approximate solution  $p$  or
%          a message that the algorithm fails.
%
% -----clean up -----
clear all; close all; clc
% -----

% Change function  $g$  for a new problem
g = @(x) sqrt(10/(x+4));

% -----initialize the problem-----
% initial guess
p0 = 1.5;
% tolerance
TOL = 1e-9;
% maximum number of iterations
NI = 100;
% -----

% -----output on screen -----
fprintf('\n Fixed Point Iteration')
fprintf('\n\n I          P\n')

% STEP 1
i = 1;
converge = false; % convergence flag

% STEP 2
while i<=NI
    % STEP 3
    % compute  $p(i)$ 
    p = g(p0);
    err = abs(p-p0); % err =  $|p\{N\}-p\{N-1\}|$ 

    % print out all intermediate approximations
    fprintf('%3i    %.9f\n', i, p)

    % STEP 4
    % check if meets the stopping criteria

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    if (err< TOL)
        converge = true;
        break
    else
        % STEP 5
        i = i+1;
        % STEP 6
        p0 = p; % update p0
    end
end

if converge
    fprintf('\n\nApproximate solution P = %.8f\n',p)
    fprintf('Number of iterations = %3i\n',i)
    fprintf('Tolerance = %.3e |p-pold| = %.3e\n',TOL, err)
else
    fprintf('\n\nInteration number = %3i\n',NI)
    fprintf(' gave approximation %.8f\n',p)
    fprintf('|p-pold| = %.3e not within tolerance %.3e\n',err, TOL)
end

```

*Fixed Point Iteration*

<i>I</i>	<i>P</i>
1	1.348399725
2	1.367376372
3	1.364957015
4	1.365264748
5	1.365225594
6	1.365230576
7	1.365229942
8	1.365230023
9	1.365230012
10	1.365230014
11	1.365230013

*Approximate solution P = 1.36523001*  
*Number of iterations = 11*  
*Tolerance = 1.000e-09 |p-pold| = 1.661e-10*

*Published with MATLAB® R2019a*