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%
% Newton-Raphson ALGORITHM 2.3
%
% To find a solution to  $f(x) = 0$  given an
% initial approximation p0
%
% This code solve Example 1 on Page 68 of the textbook.
%
% INPUT:  initial approximation p0; tolerance TOL;
%         maximum number of iterations NI.
%
% OUTPUT: approximate solution p or
%         a message that the algorithm fails.
%
% -----clean up -----
clear all; close all; clc
% -----

% Change function f and df for a new problem
f = @(x) cos(x) -x;
df = @(x) -sin(x)-1; % function derivative

% -----initialize the problem-----
% initial guess
p0 = pi/4;
% tolerance for |p-p0|
TOL = 1e-10;
% maximum number of iterations
NI = 100;
% -----

% -----output specification -----
fprintf("\nNewton's Method")
fprintf('\n\n I          P\n')

% STEP 1
i = 1;
converge = false; % convergence flag

% STEP 2
while i<=NI
    % STEP 3
    % compute p(i)
    p = p0-f(p0)/df(p0);
    err = abs(p-p0);
    % print out all intermediate approximations
    fprintf('%3i    %.9f\n', i, p)

    % STEP 4
    % check if meets the stopping criteria
    if (err< TOL)

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        converge = true;
        break
    else
        % STEP 5
        i = i+1;
        % STEP 6
        p0 = p; % update p0
    end
end

if converge
    fprintf('\n\nApproximate solution P = %.8f\n',p)
    fprintf('With F(P) = %.3e\n',f(p))
    fprintf('Number of iterations = %3i\n',i)
    fprintf('Tolerance = %.3e |p-pold| = %.3e\n',TOL, err)
else
    fprintf('\n\nInteration number = %3i\n',NI)
    fprintf(' gave approximation %.8f\n',p)
    fprintf('|p-pold| = %.3e not within tolerance %.3e\n',err, TOL)
end

```

*Newton's Method*

<i>I</i>	<i>P</i>
1	0.739536134
2	0.739085178
3	0.739085133
4	0.739085133

*Approximate solution P = 0.73908513*  
*With F(P) = 1.110e-16*  
*Number of iterations = 4*  
*Tolerance = 1.000e-10 |p-pold| = 4.441e-16*

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