# Modeling Graphs with Vertex Replacement Grammars

Satyaki Sikdar, Justus Hibshman, and Tim Weninger

Department of Computer Science and Engineering University of Notre Dame {ssikdar,jhibshma,tweninge}@nd.edu

## Introduction

Arguably the most relevant task in the study of graphs is the identification, extraction, and representation of the small substructures that, in aggregate, describe the underlying phenomenon encoded by the graph. From an extracted model, containing the LEGO-like building blocks of real-world graphs, we expect to perform deep scientific analysis and make predictions about the data.

# **Context Free Grammars**

String Grammars  $S \rightarrow NP VP$   $NP \rightarrow the N$   $VP \rightarrow V NP$   $V \rightarrow sings | eats$  $N \rightarrow cat | song | canary$  Vertex Replacement Grammars



#### **One Iteration of Extraction with** $\lambda = 3$







(d) The RHS is a non-terminal of size 5 corresponding to the 5 boundary edges in (c).



(e) Updated graph with *{c, d, e}* replaced by the non-terminal of size 5.

(b) Dendrogram *D* of H. Node  $\eta_6$  has

exactly  $\lambda$  leaf nodes {*c*, *d*, *e*}.



(c) *H* with highlighted nodes {*c*, *d*, *e*}. The 5 boundary edges are in red.



(f) Updated dendrogram with subtree rooted at  $\eta_6$  replaced by the new non-terminal.

#### **Extracted Rules**









## **Graph Generation**

## Main Results





### Conclusion

A potentially significant benefit from the VRG model stems from its ability to directly encode local substructures and patterns in the RHSs of the grammar rules. Forward applications of VRGs may allow scientists to identify previously unknown patterns

in graph datasets representing important natural or physical phenomena. Further investigation into the nature of the extracted rules and their meaning (if any) is a top priority.

#### **Related Works**

Aguinaga S, Chiang D, Weninger T (2018) *Learning hyperedge replacement grammars for graph generation*. IEEE Transactions on Pattern Analysis and Machine Intelligence pp 1–1, DOI 10.1109/TPAMI.2018.2810877

Pennycuff C, Sikdar S, Vajiac C, Chiang D, Weninger T (2018) *Synchronous hyperedge replacement graph grammars*. In: International Conference on Graph Transformation, Springer, pp 20–36



The work has been submitted to the Journal Track of ECML-PKDD 2019. The authors are supported by a grant from the US National Science Foundation (#1652492).



