

Terahertz multiheterodyne spectroscopy using laser frequency combs

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The terahertz region is of great importance for spectroscopy since many molecules have absorption fingerprints there. Frequency combs based on terahertz quantum cascade lasers feature broadband coverage and high output powers in a compact package, making them an attractive option for broadband spectroscopy. Here, we demonstrate the first multiheterodyne spectroscopy using two terahertz quantum cascade laser combs. Over a spectral range of 250 GHz, we achieve average signal-to-noise ratios of 34 dB using cryogenic detectors and 24 dB using room-temperature detectors, all in just 100 μ s. As a proof of principle, we use these combs to measure the broadband transmission spectrum of etalon samples and show that, with proper signal processing, it is possible to extend the multiheterodyne spectroscopy to quantum cascade laser combs operating in pulsed mode. This greatly expands the range of quantum cascade lasers that could be suitable for these techniques and allows for the creation of completely solid-state terahertz laser spectrometers. © 2016 Optical Society of America

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Terahertz radiation, light whose frequency lies in the 0.1–10 THz range, is of great importance for spectroscopy since many molecules have strong rotational and vibrational resonances in this frequency range. As a result, much effort has been spent developing terahertz spectroscopic techniques to address the tradeoff between detection bandwidth, frequency resolution, and acquisition time. Fourier domain techniques such as Fourier Transform infrared spectroscopy and terahertz time-domain spectroscopy (THz-TDS) are intrinsically broadband [1], but their average power is quite low; moreover, their operations typically require a mechanical moving stage to achieve maximum signal-to-noise ratios (SNRs). Impressive results have also been achieved with electronic THz sources based on cascaded frequency multiplication [2,3],

but these sources suffer parasitic roll-offs and lower power levels, especially at higher frequencies. Tunable laser sources based on high-power terahertz quantum cascade lasers (QCLs) [4] are another alternative: by tuning the source, one can reconstruct the sample's absorption feature over the tuning span [5] or conduct heterodyne detection [6]. These approaches can achieve high frequency resolution, but are usually narrowband owing to the limited tunability of the source. THz sources based on intracavity difference-frequency generation [7,8] can be broadly tuned but only offer microwatt power levels when operated in continuous-wave mode.

In contrast, multiheterodyne spectroscopy based on two frequency combs [9,10], also known as dual-comb spectroscopy, offers an elegant way of conducting broadband spectroscopy, featuring broad spectral coverage, high frequency resolution, and high signal-to-noise ratios obtained over short acquisition times, all without mechanical moving parts [11,12]. The principle is illustrated in Fig. 1(a): by beating two combs with slightly different repetition rates onto a single fast detector, one can measure a multitude of down-converted radio frequency (RF) beatnotes, each of which corresponds uniquely to the optical frequency beatings between adjacent lines from different combs. If one comb is shined through a sample, the sample's absorption information at optical frequencies is encoded in the RF spectrum.

Traditionally, frequency combs have been generated in the THz range by downconversion of ultrafast laser pulses, which forms time-domain THz pulses with well-defined phases [13,14]. More recently, there has been great interest in THz combs based on quantum cascade lasers, which are generated by nonlinearities in low-dispersion cavities [15,16]. Such combs can be generated by deliberate dispersion engineering of the laser cavity [17] or by utilizing the naturally low dispersion of the gain medium at a particular bias [18–20]. From a spectroscopy perspective, QCL-based frequency combs offer compactness, continuous-wave (CW) operation, and high output powers. Moreover, their nonpulsed nature makes them less prone to the detector saturation and gives them a larger dynamic range [21,22]. Here, we present the first demonstration of the use of THz QCL combs to perform multiheterodyne spectroscopy.

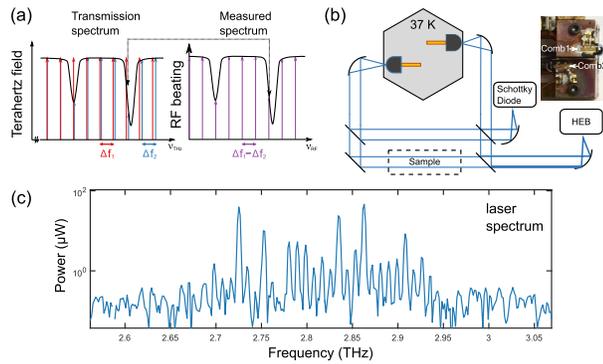


Fig. 1. (a) Multiheterodyne spectroscopy using two frequency combs with slightly different repetition rates. (b) Experimental setup. Inset shows real laser frequency combs on the copper mount, both of which are silicon lens-coupled. (c) Lasing spectrum of one device under comb operation.

Figure 1(b) shows a simplified experimental setup used for this demonstration. For simplicity, only the optical path is illustrated here; see the Supplement 1 for more detail. Using integrated dispersion compensation, two THz QCL combs were fabricated using a gain medium similar to the one in [19]. Both lasers were lens-coupled and had submilliwatt output powers at 37 K; when biased into the comb regime, their lasing spectra covered approximately 250 GHz at 2.8 THz [shown in Fig. 1(c)]. To minimize their environmental differences, both devices were mounted inside the same pulsed-tube cryocooler. To account for amplitude fluctuations, a balanced detection scheme was employed using one superconducting hot-electron bolometer (HEB) mixer [23] as the signal detector and one Schottky mixer (Virginia Diode's WR-0.34HM) as the reference detector. Naturally, the two detectors were quite different in terms of sensitivity and dynamic range—each detector must be both fast and sensitive, a challenging requirement in the terahertz range—and so some differences will be evident in the resulting measured spectra. In particular, the Schottky mixer is operated at room temperature and is less sensitive, whereas the HEB is helium-cooled and is more sensitive but also significantly less linear.

Both QCLs were biased into a comb regime and the repetition rate beatnotes were detected from them using a bias tee and are shown in Fig. 2(a). The free-running combs featured repetition rates around 9.1 GHz and were separated by a 36 MHz difference, i.e., $\Delta f_2 - \Delta f_1 = 36$ MHz. At the same time, we detected a multiheterodyne RF signal centered at 2.2 GHz from both the HEB and the Schottky mixer, indicating that these two combs' offset frequency differed by about 2.2 GHz, i.e., $f_{\text{ceo},2} - f_{\text{ceo},1} = 2.2$ GHz. The multiheterodyne signals were downconverted into the oscilloscope's bandwidth by IQ demodulating with a synthesizer, and both the in-phase and in-quadrature signals were then recorded with a fast oscilloscope.

The downconverted multiheterodyne signals were recorded for a duration of 100 μs and are shown in Figs. 2(b) and 2(c). Absolute power is expressed at the oscilloscope, and relative power is expressed with respect to the system's white noise. The signal from the HEB was used to generate a phase and timing correction signal [24,25], and this signal was used to correct both interferograms [14,26,27]. Note that while this procedure generates only two correction frequencies, because the radiation has the highly

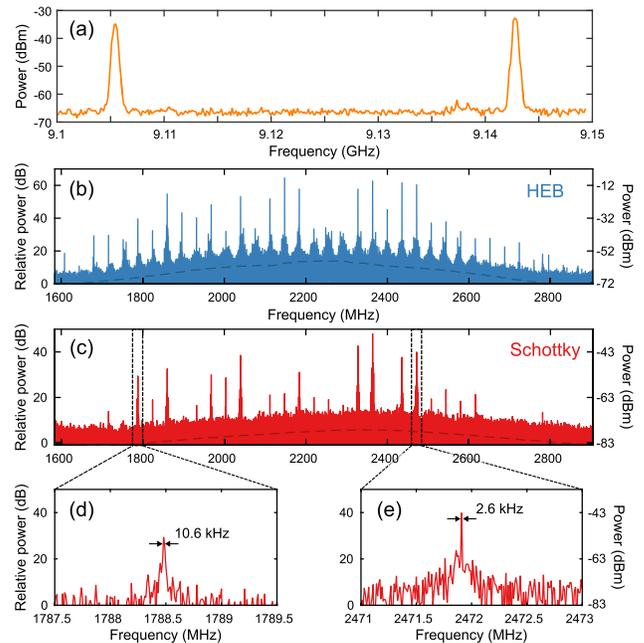


Fig. 2. (a) Repetition rates of two combs detected from a bias tee. The two repetition-rate beatnotes are located at around 9.1 GHz, with a difference of about 36 MHz. (b) Multiheterodyne signal on the HEB with a 100 μs acquisition time, with the effective noise floor indicated by a dashed line. (c) Schottky mixer signal during the same time. (d), (e) Zoomed-in view of multiheterodyne teeth from Schottky mixer at 1788.5 and 2472 MHz, respectively. The FWHM of the 1788.5 MHz tooth is 10.6 kHz and the FWHM of the 2472 MHz tooth is 2.6 kHz.

coherent structure of a comb, only two frequency parameters are needed to correct all of the multiheterodyne lines. For example, Figs. 2(d) and 2(e) show two multiheterodyne teeth from the Schottky mixer, located at 1788.5 and 2472 MHz, which have full width half-maximum (FWHM) linewidths of 10.6 kHz and 2.6 kHz, respectively. Both linewidths are at the Fourier uncertainty limit, implying that our correction procedure has removed most of the phase and timing errors. (Note also that because phase correction deletes mutual phase fluctuations, limitations in the linewidth imposed by quantum fluctuations [28,29] do not pertain here.) The leftover multiplicative noise after the phase and timing correction contributes to the noise floor of both multiheterodyne signals, forming a noise pedestal indicated by dashed lines in Figs. 2(b) and 2(c).

With an acquisition time of 100 μs , the average SNR from the HEB is about 34 dB, and the apparent dynamic range (DNR) is 52 dB. The multiheterodyne signal spans 1.08 GHz with 30 distinguishable teeth, corresponding to optical spectrum coverage greater than 250 GHz at 2.8 THz. The signal from the Schottky mixer has an average SNR of 24 dB and a DNR of 42 dB, although fewer lines are present than are visible from the HEB. As previously discussed, the difference between the signals from the two detectors mainly represents their differences in sensitivity, spectral response, and nonlinearity. In particular, saturation of the HEB generates several lines not present on the Schottky mixer, limiting its practical dynamic range to about 37 dB. Still, both detectors are clearly suitable for detecting strong multiheterodyne signals.

As a demonstration of broadband spectroscopy, we have performed transmission measurements of a low-finesse etalon made

from a tilted 625 μm thick undoped GaAs wafer. The signal and LO lasers were shined onto the HEB, and the etalon was placed in the signal laser's path. For this measurement, no reference detector was used. Figure 3(a) shows the multiheterodyne data collected from the HEB over 300 μs with and without the etalon, in blue and red, respectively. Figure 3(b) shows the ratio of individual multiheterodyne peaks along with the simulated transmission data at the frequencies that were sampled. To account for dynamic range limitations of the HEB, we plotted only those transmission values corresponding to the largest 24 lines, whose reference signal was greater than the peak intensity minus 37 dB. Periodic transmission due to the etalon is clearly visible within the lasing spectral range, and is in reasonable agreement with the theoretically calculated etalon transmission. Because no reference detector was used, some residual errors were present on account of relative intensity fluctuations that occurred between the two measurements with and without the sample.

Last, we examine the feasibility of multiheterodyne spectroscopy based on QCLs which are operated in pulsed biasing mode (not to be confused with the optical pulses of a mode-locked laser). It is well known that operating QCLs in continuous-wave mode is significantly more challenging than operating the same devices in pulsed mode, because CW operation places much greater thermal constraints on the laser in both the midinfrared and the terahertz. Many gain media simply have thresholds that are too high for CW operation and, even when CW operation is possible, the lasers' power dissipation becomes problematic. For dual-comb THz spectroscopy, this is doubly problematic because the two lasers are placed inside the same cooler. In addition, it is often desirable for spectroscopy to have small repetition rates, as the dense mode spacing eases the constraints on the detector and also makes it easier to achieve gapless coverage. Unfortunately, this necessarily entails longer lasers that consume more power. As an example, we constructed 7 mm combs from the gain medium of [17], which consume approximately 1.3 A ($\sim 1000 \text{ A/cm}^2$) and 15 V. Although these lasers have small free spectral ranges, around 4.8 GHz, the two of them together consume $\sim 40 \text{ W}$.

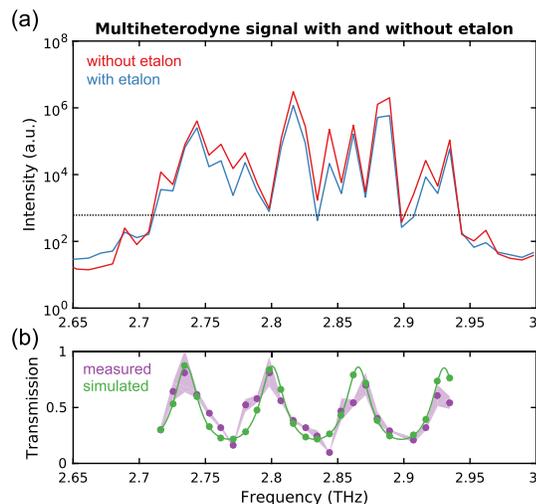


Fig. 3. (a) Intensity of individual multiheterodyne peaks with and without the GaAs etalon. The dashed horizontal line indicates the threshold for inclusion in the transmission data. (b) Measured etalon transmission (in purple) and the simulated etalon transmission (in green). The shaded region indicates one standard deviation.

This constitutes a major load on the cryocooler and would result in the lasers warming to above their maximum CW operating temperature.

Traditionally, pulsed mode operation of QCLs is considered anathema to multiheterodyne spectroscopy, as dual comb spectroscopy usually requires stable combs while pulsed-mode operation is inherently unstable. However, by using self-referenced SWIFTS [30] to evaluate the coherence of similar devices, we have previously shown that even extremely unstable devices usually maintain their mutual coherence, at least in the most general sense that the modes remain evenly spaced. This implies that by applying the same phase and timing correction techniques previously described, we should be able to recover multiheterodyne lines even in the face of the large instability and chirp associated with pulsed operation. Although the absolute chirp of the lasers remains unknown, impeding the analysis of high-resolution features, it may alternatively be possible to exploit this effect to perform high-resolution spectroscopy [31].

Figure 4 shows the results of pulsed-mode, dual-comb spectroscopy using the aforementioned devices, whose gain media and dispersion compensation scheme are described in [17]. The lasers are biased to a comb regime using 120 μs pulses with a repetition frequency of 100 Hz, resulting in a duty cycle of 1.2%. This low duty cycle significantly eases the cryogenic operation. A low-pass filter was used to select only the part of the comb spectrum around 3.3 THz. Figures 4(a) and 4(d), respectively, show in the time domain the combs' repetition rate signal (measured from a bias tee) and corresponding multiheterodyne signal (measured from the HEB). As expected, both signals turn on during the electrical pulse, but while the electrical repetition rate beatnotes turn on within a few μs , the optical multiheterodyne signal takes approximately 30 μs to stabilize. This reflects the fact that electrical beatnotes are unreliable indicators of optical beatnotes. Figure 4(c) shows the distinct repetition rate beatnotes in the frequency domain, clearly showing their frequency difference of 10 MHz. In pulsed mode, chirping of the repetition rate due to device heating is noticeable; this heating results in a substantial broadening of the beatnote indicated by red in Fig. 4(c). (The lasers have slightly different beatnotes due to differences in the dispersion compensation and lens mounting, and the one indicated by blue possesses less chirp).

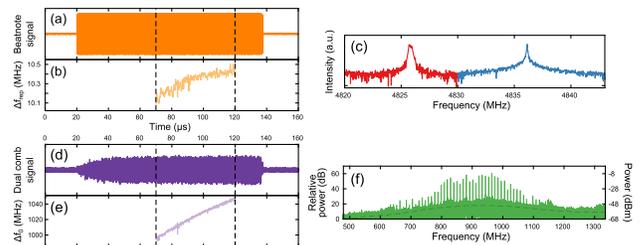


Fig. 4. (a) Time domain signal of combs' repetition rate measured electrically from a bias tee. (b) Chirping of the repetition rates' difference. (c) Frequency domain signal of combs' repetition rate measured electrically from a bias tee; they are located around 4.8 GHz and spaced by 10 MHz. (d) Time domain signal of the multiheterodyne signal measured from the HEB detector. (e) Chirping of the multiheterodyne signal's offset frequency in the interval indicated by the dashed lines. (f) Multiheterodyne signal in the frequency domain, centered at 900 MHz with 45 observable modes, with the effective noise floor indicated by a dashed line.

When the difference in their repetition rates is plotted in the time domain, as shown in Fig. 4(b), the chirp due to heating is evident. During the 50 μ s period indicated by the two dashed lines, the difference of the combs' repetition rates gradually increases from 10.1 to 10.5 MHz. In addition, Fig. 4(c) shows the chirp of the offset frequency difference during the same 50 μ s; it too is up-chirped. However, its magnitude is much larger, over 40 MHz, which is approximately 100 times the repetition rate chirping. (Of course, quantifying the absolute frequency of each laser remains impossible without an absolute frequency reference.) Last, Fig. 4(f) shows the phase- and timing-corrected multiheterodyne signal in the frequency domain. The repetition rate difference of 10 MHz is clearly visible here and over 45 modes are contributing to the multiheterodyne signal, implying a coverage of 215 GHz in the THz spectrum. Within 50 μ s of integration, the average SNR of the multiheterodyne signal is higher than 25 dB on the HEB. Of course, co-averaging multiple pulses further boosts the SNR.

In conclusion, we have demonstrated the first THz multiheterodyne spectroscopy using quantum cascade laser frequency combs. The spectral coverage is 250 GHz at 2.8 THz, limited by the bandwidth of the lasing spectrum, and as a proof-of-principle we have used them to measure the transmission of etalon samples. As broadband gain media designs continue to develop, we expect much broader coverage of the THz spectrum. Moreover, we have shown that even under pulsed-mode operation, laser frequency combs are still feasible for multiheterodyne spectroscopy. Pulsed-mode multiheterodyne spectroscopy shows great promise for reducing the cooling power constraints, allowing for the use of compact Stirling cryocoolers. Together with room-temperature Schottky mixers as detectors, this will enable a very compact spectroscopy system at the THz region.

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See Supplement 1 for supporting content.

REFERENCES

- I. A. Finneran, J. T. Good, D. B. Holland, P. B. Carroll, M. A. Allodi, and G. A. Blake, *Phys. Rev. Lett.* **114**, 163902 (2015).
- B. Drouin, F. W. Maiwald, and J. Pearson, *Rev. Sci. Instrum.* **76**, 093113 (2005).
- J. C. Pearson, B. J. Drouin, A. Maestrini, I. Mehdi, J. Ward, R. H. Lin, S. Yu, J. J. Gill, B. Thomas, C. Lee, G. Chattopadhyay, E. Schlecht, F. W. Maiwald, P. F. Goldsmith, and P. Siegel, *Rev. Sci. Instrum.* **82**, 093105 (2011).
- Q. Qin, B. S. Williams, S. Kumar, J. L. Reno, and Q. Hu, *Nat. Photonics* **3**, 732 (2009).
- S. Bartalini, L. Consolino, P. Cancio, P. De Natale, P. Bartolini, A. Taschin, M. De Pas, H. Beere, D. Ritchie, M. S. Vitiello, and R. Torre, *Phys. Rev. X* **4**, 021006 (2014).
- Y. Ren, J. N. Hovenier, R. Higgins, J. R. Gao, T. M. Klapwijk, S. C. Shi, B. Klein, T.-Y. Kao, Q. Hu, and J. L. Reno, *Appl. Phys. Lett.* **98**, 231109 (2011).
- Q. Y. Lu, S. Slivken, N. Bandyopadhyay, Y. Bai, and M. Razeghi, *Appl. Phys. Lett.* **105**, 201102 (2014).
- Y. Jiang, K. Vijayaraghavan, S. Jung, A. Jiang, J. H. Kim, F. Demmerle, G. Boehm, M. C. Amann, and M. A. Belkin, *Sci. Rep.* **6**, 21169 (2016).
- S. Schiller, *Opt. Lett.* **27**, 766 (2002).
- F. Keilmann, C. Gohle, and R. Holzwarth, *Opt. Lett.* **29**, 1542 (2004).
- I. Coddington, W. C. Swann, and N. R. Newbury, *Phys. Rev. Lett.* **100**, 013902 (2008).
- N. R. Newbury, I. Coddington, and W. Swann, *Opt. Express* **18**, 7929 (2010).
- M. Tonouchi, *Nat. Photonics* **1**, 97 (2007).
- T. Yasui, R. Ichikawa, Y.-D. Hsieh, K. Hayashi, H. Cahyadi, F. Hindle, Y. Sakaguchi, T. Iwata, Y. Mizutani, H. Yamamoto, K. Minoshima, and H. Inaba, *Sci. Rep.* **5**, 10786 (2015).
- A. Hugi, G. Villares, S. Blaser, H. C. Liu, and J. Faist, *Nature* **492**, 229 (2012).
- J. B. Khurgin, Y. Dikmelik, A. Hugi, and J. Faist, *Appl. Phys. Lett.* **104**, 081118 (2014).
- D. Burghoff, T.-Y. Kao, N. Han, C. W. I. Chan, X. Cai, Y. Yang, D. J. Hayton, J.-R. Gao, J. L. Reno, and Q. Hu, *Nat. Photonics* **8**, 462 (2014).
- M. Wienold, B. Roben, L. Schrottké, and H. T. Grahn, *Opt. Express* **22**, 30410 (2014).
- M. Rosch, G. Scalari, M. Beck, and J. Faist, *Nat. Photonics* **9**, 42 (2015).
- H. Li, P. Laffaille, D. Gacemi, M. Apfel, C. Sirtori, J. Leonardon, G. Santarelli, M. Rosch, G. Scalari, M. Beck, J. Faist, W. Hansel, R. Holzwarth, and S. Barbieri, *Opt. Express* **23**, 33270 (2015).
- Y. Wang, M. G. Soskind, W. Wang, and G. Wysocki, *Appl. Phys. Lett.* **104**, 031114 (2014).
- G. Villares, A. Hugi, S. Blaser, and J. Faist, *Nat. Commun.* **5**, 5192 (2014).
- W. Zhang, P. Khosropanah, J. R. Gao, E. L. Kollberg, K. S. Yngvesson, T. Bansal, R. Barends, and T. M. Klapwijk, *Appl. Phys. Lett.* **96**, 111113 (2010).
- Y. Yang, "Towards THz dual-comb spectrometer based on quantum cascade laser frequency combs," presented at International Conference on Intersubband Transitions in Quantum Wells, Vienna, Austria (September 6–11, 2015).
- D. Burghoff, Y. Yang, and Q. Hu are preparing a manuscript to be called "Computational multiheterodyne spectroscopy."
- J. Roy, J.-D. Deschenes, S. Potvin, and J. Genest, *Opt. Express* **20**, 21932 (2012).
- T. Ideguchi, A. Poisson, G. Guelachvili, N. Picque, and T. W. Hansch, *Nat. Commun.* **5**, 3375 (2014).
- M. S. Vitiello, L. Consolino, S. Bartalini, A. Taschin, A. Tredicucci, M. Inguscio, and P. De Natale, *Nat. Photonics* **6**, 525 (2012).
- S. Bartalini, S. Borri, P. Cancio, A. Castrillo, I. Galli, G. Giusfredi, D. Mazzotti, L. Gianfrani, and P. De Natale, *Phys. Rev. Lett.* **104**, 083904 (2010).
- D. Burghoff, Y. Yang, D. J. Hayton, J.-R. Gao, J. L. Reno, and Q. Hu, *Opt. Express* **23**, 1190 (2015).
- M. Nikodem and G. Wysocki, *Sensors* **12**, 16466 (2012).